COUPLING MECHANISM OF VOLUME STRAIN AND WATER LEVEL IN THE FUXIN WELL LOCATED IN A GEOTHERMAL AREA BEFORE AND AFTER THE 2011 $M_w$ 9.1 TOHOKU EARTHQUAKE

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ABSTRACT

According to previously reported observations, low-frequency (~0.01–500 Hz) seismic waves can enhance permeability and alter the distribution of pore pressure, which in turn, enhance geothermal energy/oil production. To quantify the effects of low-frequency, dynamic stress stimulation on fluid flow and in-situ pore pressure variations in porous media, observations were conducted in the Fuxin well (located in a geothermal area in north-eastern China), before and after the far-field $M_w$ 9.1 Tohoku huge earthquake. In doing so, precise measurements of earthquake-induced stress, strain, aquifer characteristics and fluid flow parameters could be obtained. We apply tidal analysis to the volumetric strain and water level data of the well. We demonstrate that the tele-seismic waves with a central frequency of 0.02 Hz hardly had an impact on the undrained poroelastic parameters of the aquifer, indicating that the tele-seismic waves cannot induce the disruption of the aquifer medium directly, although it can easily enhance permeability and induce the transfer of pore pressure in the aquifer. Together with the phases, the signs of the co-seismic amplitude change as well as the co-seismic and post-seismic patterns of volumetric strain and water level, we obtain the coupling mechanism of the volume strain change and the water level change: Before the earthquake, tidal volumetric strain induced the change of water level (the phase of the water level lagged behind that of the volume strain). In comparison, during the earthquake, the permeability enhanced by tele-seismic waves, water level (pore pressure) transferred from high pressure region to the Fuxin well, and induced the dilatation of volume strain (phase shifts increased sharply, indicating the change of water level caught up with that of volume strain). Finally, during the short time span after the earthquake, the water level and volumetric strain interacted with each other and changed consistently (phase shifts approach 0°).

1. INTRODUCTION

During geothermal exploration, injection of water into geothermal reservoirs induces thermo- and poroelastic stresses, and causes reservoir deformations. Pore pressure alters the effective stress acting on the rock, which influences rock fracture (Hassanzadegan et al., 2011). It has been repeatedly observed that low-frequency (~0.01–500 Hz) seismic waves can enhance permeability (e.g. Brodsky et al., 2003; Elkhoury et al., 2006; Zhang et al., 2015a; Zhang et al., 2015b), and then alter the distribution of pore pressure, which enhances oil production from depleted reservoirs and contaminant extraction from groundwater aquifers. To quantify the effects of low-frequency, dynamic stress stimulation on fluid flow and in situ pore pressure variations in porous media, in-situ observations that enabled precise measurement of earthquake-induced stress, strain, aquifer and fluid flow parameters should be conducted.

Several recent studies show that the co-seismic change in volumetric strain measured in the far field of large earthquakes is often far greater than that predicted from static strain theory (e.g. Fu et al., 2011; Zhang et al., 2014; Zhang et al., 2015a). The underlying reason for this disparity between measurement and theory is not yet understood, mainly because of the expense in drilling and installing scientific boreholes, but it is important for the interpretation of strain data. According to the theory of linear poroelasticity (Wang, 2000), the pressure perturbation in an undrained medium is proportional to the dilatational stress imposed on it (Roeloffs, 1996). Barbour (2015) analysed records of dynamic strain and pore pressure from regional and tele-seismic earthquakes at Plate Boundary Observatory stations and found robust scaling response coefficients between excess pore pressure and dynamic strain at each station that are spatially correlated.

As studied by Kilb et al (2002), in the near-field (near field: epicentral distance < 1 fault rupture length; far field: epicentral distance >1000 km) both the static and dynamic stresses are comparable in

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magnitude, however, in the far field, the peak dynamic stress is far greater than the static change. Thus, we may infer that the far-field variation of volume strain and water level (pore pressure) may be related to dynamic shaking by tele-seismic waves. As has been studied before, fracture clearing (unclogging) and permeability increase, induced by dynamic stress due to the propagation of tele-seismic waves, have been widely used to explain most documented far-field water level (pore pressure) changes (e.g. Brodsky et al., 2003; Elkhoury et al., 2006; Wang and Chia, 2008; Wang and Manga, 2009; Xue et al., 2013; Lai et al., 2013; Zhang et al., 2015b; Shi et al., 2014a, b; Shi et al., 2015). In addition, the size of the pressure response is generally expected to correlate with the level of seismic energy density (e.g. Wang and Chia, 2008; Zhang et al., 2015a; Lai et al., 2016). As indicated by Manga et al. (2012), in natural systems, strain amplitudes as small as $10^{-6}$ can enhance permeability.

The borehole strain metre in the Fuxin well offers an excellent opportunity to test for variation in volume strain response to the tele-seismic waves of great earthquakes and to detect the coupling mechanism between the volume strain and the water level. As previously studied, this well is extremely sensitive to great earthquakes (magnitude $> M_s 8.0$) occurring in far fields (epicentral distances $> 1000$ km) (Zhang et al., 2015a). Here we apply tidal analysis to the volumetric strain and water level data recorded in the well, before and after the 2011 $M_w 9.1$ Tohoku earthquake. We find that tele-seismic waves with a central frequency of 0.02 Hz hardly had an impact on the undrained poroelastic parameters of the aquifer, suggesting that the tele-seismic waves cannot induce the disruption of the aquifer medium directly, although it can easily enhance the permeability and induce the transfer of pore pressure in the aquifer. Together with the phases, the signs of the co-seismic amplitude change as well as the co-seismic and post-seismic patterns of volumetric strain and water level, we obtain the coupling mechanism of the volume strain change and the water level change. Before the earthquake, tidal volumetric strain induced the change of water level (the phase of the water level lagged behind that of the volume strain), whereas during the earthquake, the permeability enhanced by tele-seismic waves, water level (pore pressure) transferred from high pressure region to Fuxin well, and induced the dilatation of volume strain (phase shifts increase sharply, indicating the change of water level caught up with that of volume strain). Moreover, during the short time span after the earthquake, the water level and volumetric strain interacted with each other and changed consistently (phase shifts approach 0°). In addition, we also find that a dynamic energy density of $\sim 5 \times 10^{-2}$ J/m$^3$, which resulted from the shaking by tele-seismic waves from the far-field Tohoku earthquake (computed from broadband seismograms), could indirectly incur a dilatation stress of $\sim 0.0176$ MPa in the Fuxin well aquifer. As the Fuxin well lies in a geothermal area, this study’s findings may also have implications for geothermal resource exploration.

2. OBSERVATIONS

The Fuxin well (Fig. 1) is located in Fuxin City, Liaoning Province, northeastern China and in the northwest Fuxin Graben Basin. The region near the well lies at a tectonic cross-section between the Yinshan and Neocathaysian structural belts. The depth of the Fuxin well is 60.74 m. The stratigraphy at the well is as follows: 0–15 m is a relatively unconsolidated formation; 0–1.5 m is Quaternary
Table 1 occurrence, epicentral distance, observed co-seismic volume strain and water level changes at the Fuxin well for the 2011 Mw 9.1 Tohoku earthquake. The static co-seismic change of volume strain is calculated based on the elastic half-space dislocation model (Okada, 1992; Lin and Stein, 2004; Toda et al., 2005). The background variability of observed volume strain is computed as a standard deviation of continuous observation data during the 2.5 months before the earthquake. For the volumetric strain change, the symbol ‘+’ indicates dilatation, otherwise compaction is indicated.

<table>
<thead>
<tr>
<th>Epicenter</th>
<th>Occurrence time (Beijing)</th>
<th>Epicentral distance (km)</th>
<th>Background variability of observed volume strain (10⁻⁹)</th>
<th>Observed co-seismic volume strain change (10⁻⁹)</th>
<th>Observed co-seismic water level change (cm)</th>
<th>Static co-seismic change of volume strain (10⁻⁹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tohoku</td>
<td>13:47:32.8</td>
<td>1236.09</td>
<td>45.87</td>
<td>195.2</td>
<td>42.2</td>
<td>10.00</td>
</tr>
<tr>
<td></td>
<td>11 March 2011</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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</tbody>
</table>

A TJ–2 type strain-gauge was installed at the bottom of the well to measure volume strain; its observational sensitivity ≥ 2.0 mV/10⁻⁹, resolution ratio ≤ 1×10⁻⁹ and noise level < 0.1 mV. It has been working since April 1st, 2001 and records the Earth tides clearly and stably. Other down-hole digital instruments include a water level gauge and a barometric gauge, with sensitivity of 1 cm/mV and 1 hPa/mV respectively. It should be stressed that the water level instrument used to acquire hourly data has been set to record data every minute since 2009.

As an artesian well with the aquifer confined, the water level measurements are directly related to the changes in pore pressure. Based on the datasets, we used Mapsis software (Lu et al., 2002) to calculate the theoretical Earth tides (tidal volumetric strains). Table 1 lists some basic earthquake parameters, co-seismic strain/water level datasets and background (pre-earthquake) volume-strain variabilities. Figure 2 (a) compares the original volume-strain, water level and Earth tide and atmospheric pressure variations observed in the Fuxin well before and after the 2011 Mw 9.1 Tohoku earthquake. We see that both the volume and water level show obvious co-seismic response to this far-field large earthquake. To compare the volumestrain and water level variations directly, the original datasets shown in Figure 2 (a) are corrected by removing the trend, the influence of tidal strain and atmospheric pressure using a harmonic analysis method based on the Fourier transform and wavelet decomposition (Yan et al., 2007), with the results shown in Figure 2 (b). According to the monitoring records of Fuxin station, the co-seismic volumetric strain variation induced by the 2011 Mw 9.1 Tohoku earthquake has been corrected. Long-time span original water level and volume strain before and after this earthquake are shown in (Appendix-Fig. 2).

3. CALCULATION OF THE CO-SEISMIC STATIC STRAIN CHANGE

Using the elastic half-space dislocation model (Okada, 1992; Lin and Stein, 2004; Toda et al., 2005), we calculated the co-seismic static strain change in the Fuxin well (Fig. 3; Table 1). We see that the static volume strain changed slightly during the earthquake, much less than the observed co-seismic volume strain. This implies that the co-seismic volume strain variation cannot be attributed to the variation in the co-seismic static strain. The dynamic stress due to the huge earthquake might be used to explain the mechanism. Based on our observed data, the variation in volume strain 2004 - 2008 ranges from -873359.8 × 10⁻⁹ to 408232.4 × 10⁻³, with the amplitude change ranging from 1.0 × 10⁻⁹ to 873359.8 × 10⁻⁹. Using the general range of elastic moduli for some typical rocks (Liu and Tang, 1998), we set the dynamic elastic modulus to E = 90 GPa for the bedrock (stiff granites). Using the observed volume strain change (Δεv), we can compute the co-seismic stress change Δσ_v = EΔε_v = 0.017568 MPa. As indicated by King et al. (1999), fracture of an impermeable fault can be induced in the far field. According to Chen and Huang (2001), the ranges in compression and tensile strength as failure limits for typical granites are 200–300 MPa and 4–7 MPa, respectively. Therefore, as listed in Table 1, the stress change induced by this great earthquake is far below the failure limit at which microcracks and damage occur.

4. SEISMOGRAMS, PEAK GROUND VELOCITY (PGV) AND ENERGY DENSITY

As indicated by Brodsky et al. (2003), only sufficient large flow velocity can result in unblocking. However, we lack observation data on induced flow velocities and high sampling rate water level records from which the flow velocity can be deduced (Wang et al., 2009). The water level records available to us are sampled at hour or minute frequencies and are not precise enough for this purpose. We have to resort to the analysis of energy density (Wang and Chia, 2008). Using a plotting software (Zhao et al., 2008), we
prepared seismograms at the SNY station (the central frequency of the tele-seismic waves received by the SNY station is 0.02 Hz), as shown in Figure 4, which were used to extract certain information correlated with the co-seismic response in the Fuxin well. The distance between the station and the well is about 102.81 km, short enough for both sites to experience similar effects from the tele-seismic waves. In addition, the geology at both sites is similar, with their main matrix rocks consisting of granites.

The first key parameter is the PGV of the z-component. As shown in Figure 4, the z-component PGV is approximately 6.037 mm/s for this huge earthquake. Therefore, the z-component energy density can be calculated as

\[ e = \frac{E}{V} = \frac{1/2mv_z^2}{V} = \frac{1/2(\rho sV)v_z^2}{V} = 1/2\rho sv_z^2 \]  (*)

where \( E \) is the seismic energy, \( m \) the mass, \( V \) the volume, \( v_z \) the z-component velocity and \( \rho_s = 2.65 \text{ g/cm}^3 \) is the density of the rock matrix in the well aquifer. Because of the short distance between the Fuxin well and the SNY station, the energy density (4.829×10^{-2} J/m³) could be taken as the regional value resulting from the far-field effect of the Tohoku earthquake. Based on the statistics of a global dataset from southern California, Wang and Chia (2008) show that there are sustained water level changes resulting from earthquake-enhanced permeability for an energy density between 10^{-4} J/m³ and 10^{-1} J/m³ in the far field (>1000 km). Below the threshold value, the flow velocity induced by the energy may not be large enough to promote unclogging in the aquifer. Hence, the energy density (4.829 × 10^{-2} J/m³) induced by the shaking of the 2011 Tohoku earthquake enhanced the permeability leading to a sustained water level increase in the far field (Fig. 2 (a), (b)).

5. CALCULATION OF THE AMPLITUDE RATIO AND PHASE SHIFT

Periodic changes in Earth tides cause aquifers to expand or contract, resulting in fluctuations in pore fluid pressure, leading to corresponding fluctuations of the water level in wellbores connected to confined aquifers (Hsieh et al., 1987). The amplitude and phase responses of water level to Earth tides have been used to monitor aquifer storativity and permeability, respectively (Hsieh et al., 1987; Elkhoury et al., 2006; Doan et al., 2006; Xue et al., 2013). In a confined system small phase lags result from high permeability, whereas large phase lags result from low permeability. The amplitude response is primarily a measure of specific storage.

Cooper et al. (1965) showed that the steady fluctuation of water level in a well occurs at the same frequency as the harmonic pressure head disturbance in the aquifer. However, the amplitude of the response is generally different from that of the disturbance and there is also a shift in phase. Hsieh et al. (1987) described the pressure head disturbance and water level response by

\[ h_I = h_0 \exp(\text{i}\omega t) \]  (1)

\[ x = x_0 \exp(\text{i}\omega t) \]  (2)

respectively, where \( h_I \) is the fluctuating pressure head in the aquifer; \( h_0 \) is the complex amplitude of pressure head fluctuation; \( x \) is the displacement of the water level from the static position; \( x_0 \) is the complex amplitude of the water level fluctuation; \( \omega = 2\pi \tau \) is the frequency of fluctuation; \( \tau \) is the period of fluctuation.

Complex notation is used in (1) and (2) to facilitate the theoretical development below. However, it is understood that we are interested in only the real parts of \( h_I \) and \( x \). The amplitude response \( A \) is defined as the ratio between the amplitude of the water level fluctuation and that of the pressure head fluctuation. In terms of \( x_0 \) and \( h_0 \), \( A \) can be expressed as

\[ A = \left| \frac{x_0}{h_0} \right| \]  (3)

The phase shift is defined as...
The most commonly analyzed phase is $M_2$ because of its large amplitude and relatively low contamination by barometric pressure or diurnal temperature fluctuations (Hsieh et al., 1987; Rojstaczer and Agnew, 1989; Doan et al., 2006). In this work, we also focused on the $M_2$ phase (period 745.2 min). We calculated the amplitude ratio and phase shift between the water level and the volumetric strain based on the cross-correlation method (e.g., Lai et al., 2011; Zhang et al., 2015a), with a moving time window of 30 days and a running step of 3 days (Fig. 5).

As indicated in Figure 5 and Table 2, the phase shifts increased after the 2011 Tohoku earthquake, implying a permeability increase. Hence, the coseismic water-level change mostly occurred as a result of the enhanced permeability induced by the shaking from the tele-seismic waves. According to Hsieh et al. (1987), for a homogeneous, isotropic, laterally extensive and confined aquifer, the phase shifts between Earth tides (volumetric strain) and water level are assumed to be caused by the time required for water flowing into and out of the well. In such a case, the water-table drainage effect is ignored, and the resulting phase shift should always be negative. In other words, a phase shift increase (e.g. from $-5^\circ$ to $-1^\circ$) implies an increase in transmissivity or permeability (Hsieh et al., 1987; Elkhoury et al., 2006). However, in this paper, positive phase shifts were observed after the earthquake, which might be attributed to errors. We calculated the standard deviation of the pre-earthquake phase shift to be 23.6588. Thus, the phase shifts could be 0° after the earthquake, indicating that the variation in water level caught up with that of the volumetric strain and then changed similarly and consistently.

\[
\eta = \arg \left( \frac{x_o}{h_o} \right) \quad (4)
\]

where $\arg (z)$ is the argument of the complex number $z$. The phase shift can be thought of as being $2\pi t_p / \tau$, where $t_p$ is the time lag from the moment the water level fluctuation reaches a peak to the moment the pressure head fluctuation reaches a peak.

The well response depends on the flow of water through the porous medium and therefore is sensitive to the aquifer transmissivity and storage. Transmissivity is the rate of water transmission through a unit width of aquifer under a unit hydraulic gradient and is directly proportional to permeability. Storage coefficient is the volume of water released from storage per unit decline in hydraulic head in the aquifer. Additional factors of the response in the most general case also include the well geometry, the period of oscillation and inertial effects. The inertial effects are negligible for long periods of the Earth tides (Cooper et al., 1965). The other two factors are independently well constrained. Thus, the amplitude $A$ and phase $\eta$ responses for the long periods of tidal oscillations are (Hsieh et al., 1987):

\[
A = (E^2 + F^2)^{-1/2} \quad (5)
\]

\[
\eta = -\tan^{-1}(F/E) \quad (6)
\]

where

$E = 1 - (\omega r_w^2 / 2T) \text{Kei} (\alpha), \quad F = (\omega r_w^2 / 2T) \text{Ker} (\alpha), \quad \alpha = (\omega S / T)^{1/2} r_w \quad (7)$

and $T$ is the transmissivity, $S$ is the dimensionless storage coefficient, Ker and Kei are the zero-order Kelvin functions, $r_w$ is the radius of the well (7.5 cm for Fuxin well), $r_c$ is the inner radius of the casing (6.5 cm for Fuxin well) and $\omega$ is the frequency of the tide.
Table 2 Co-seismic phases and amplitude responses from the Fuxin well for the 2011 $M_w$ 9.1 Tohoku earthquake.

<table>
<thead>
<tr>
<th>Pre-earthquake phase shift</th>
<th>Post-earthquake phase shift</th>
<th>Background phase shift variability</th>
<th>Coseismic phase shift change</th>
<th>Pre-earthquake amplitude ratio</th>
<th>Post-earthquake amplitude ratio</th>
<th>Background variability</th>
<th>Coseismic amplitude ratio change</th>
</tr>
</thead>
<tbody>
<tr>
<td>-87.606</td>
<td>-12.077</td>
<td>23.658</td>
<td>75.523</td>
<td>3.023</td>
<td>2.801</td>
<td>0.715</td>
<td>-0.222</td>
</tr>
</tbody>
</table>

Table 2 lists the co-seismic phase shift and amplitude ratio responses. The phase response means phase shifts between volumetric strain and water level, where the symbol ‘$-$’ indicates a lag of water level behind volume strain. The pre-/post-earthquake values are the respective average values of three pre-/post-earthquake points measured within 15 days of the earthquake. The background variabilities are the standard deviations of the pre-earthquake phase shifts and amplitude ratios. The co-seismic variations of phase shift / amplitude ratio are obtained by subtracting the pre-earthquake values from the post-earthquake values.

Before the earthquake, water level fluctuation in the Fuxin well had a negative phase shift as a result of the delay in groundwater flow to the well, driven by the tidal volumetric strain of the aquifer. In comparison, following the earthquake, the phase of the water level fluctuations caught up with that of the volumetric strain, suggesting that the co-seismic change in strain may reflect the co-seismic change in pore pressure (water level) in the aquifer. After the earthquake, the water level might still maintain a dynamic state, that is, continues to flow into the well or flow out of the well to recover and influence the volume strain. Meanwhile, the volume strain induced the change of water level in the manner of tidal strain. Thus, during a short time span after the earthquake, the phase shifts between the water level and the volume strain approached zero (Fig. 5), indicating that the water level and volumetric strain interacted with each other and changed consistently.

6. CALCULATION OF CONTINUOUS $BK_U$ (B: SKEMPTON’S COEFFICIENT; $K_u$: UNDRAINED BULK MODULUS) AND TRANSMISSIVITY

In the near field, where the co-seismic static strain is large and thus the measured strain is consistent with that predicted from an elastic model (Johnston and Linde, 2002). However, in the far field, the situation is different. As shown in Table 1, the co-seismic increase in the volumetric strain measured is far greater than that predicted from static strain theory. The underlying reason for this disparity is not yet understood. As analysed above, the co-seismic change in strain may reflect the co-seismic change in pore pressure (water level) in the aquifer. Thus, poroelastic theory can be used to clarify this mechanism.

For the loading of Earth tides, the periods of diurnal and semi-diurnal waves are relatively shorter compared with the time scale of the discharge and recharge time of groundwater, which could be regarded as an undrained condition (Yan, 2008). Therefore, we could evaluate the undrained parameters of the aquifer based on poroelastic-theory using the loading of the $M_2$ wave (Yan, 2008; Zhang et al., 2009; Zhang and Huang, 2011; Shi et al., 2013).

In a confined reservoir, for the linearly poroelastic media, the amplitude of pore pressure change in the aquifer, $\Delta p$, may be related to the amplitude of volumetric strain change, $\Delta \varepsilon$, by the following relationship (Doan et al., 2006):

$$\Delta p = -\frac{B \Delta \varepsilon}{3} = -BK_u \Delta \varepsilon,$$

where $K_u$ is the undrained bulk modulus, and $B$ is the Skempton coefficient. Equation (8) indicates that in the undrained condition, the change in fluid pressure $\Delta p$ is proportional to the change in volume strain $\Delta \varepsilon$. Using equation (8), we obtain the following:

$$\Delta h = \frac{-BK_u \Delta \varepsilon}{\rho g},$$

where $\rho$ is the density of water, $g$ is the gravitational acceleration, and $\Delta h$ is the change in pressure head in the aquifer. Using equations (9) and (3), we derive the following:

$$A = \frac{|x_o/\rho g|}{|x_o/\rho g|} = \frac{|x_o/\rho g|}{|x_o/\rho g|} = \frac{B K_u}{\rho g},$$

where $\varepsilon_0$ is the change in mean strain (volumetric strain). Assuming the storage coefficient $S = 10^{-2}$, this is a typical value and the most often used for aquifers as it is not sensitive to changes in phase and amplitude (e.g. Doan et al., 2006; Lai et al., 2011). On the basis of equations (5), (6), (7) and (10), and substituting the measured phase $\eta$ and the amplitude response ratio $|x_o/\varepsilon_0|$ (Fig. 5), we can derive $BK_u$ ($B$: Skempton’s coefficient; $K_u$: undrained bulk modulus) and the transmissivity $T$ (Fig. 6). In accordance with the calculation of amplitude ratio and phase shift, $BK_u$ and the transmissivity $T$ are also calculated with a moving time window of 30 days and a running step of 3 days (Fig. 6).

Table 3 lists the $BK_U$ and transmissivity values obtained in this study. As can be seen, the initial $BK_U$/transmissivity values are the average values at three pre-earthquake points, measured within 15 days of the earthquake. The background variables are the standard deviations of the pre-earthquake $BK_U$ and transmissivity values. The co-seismic $BK_U$/transmissivity changes are obtained by
Fig. 6 Transmissivity and $BK_U$ over time from the Fuxin well before and after the 2011 $M_w$ 9.1 Tohoku earthquake. The vertical dashed lines indicate the start time of the earthquake (Beijing time).

Table 3 Initial, background and co-seismic change of $BK_u$ and transmissivity from the Fuxin well for the 2011 $M_w$ 9.1 Tohoku earthquake.

<table>
<thead>
<tr>
<th></th>
<th>Initial $BK_u$/GPa</th>
<th>Background variability/GPa</th>
<th>Coseismic change/$BK_u$/GPa</th>
<th>Initial transmissivity/(m²/s)</th>
<th>Background transmissivity variability/(m²/s)</th>
<th>Coseismic transmissivity change/(m²/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2.9622</td>
<td>0.8125</td>
<td>0.7543</td>
<td>1.0519×10⁻⁶</td>
<td>7.7507×10⁻⁷</td>
<td>4.1958×10⁻⁶</td>
</tr>
</tbody>
</table>

Table 4 Pre-seismic $BK_u$, the converted co-seismic change of volumetric strain from the co-seismic change in water level, and the observed co-seismic change of volumetric strain.

<table>
<thead>
<tr>
<th>Earthquake</th>
<th>Pre-earthquake $BK_u$ (GPa)</th>
<th>Converted co-seismic change of volumetric strain from co-seismic change in water level ($10^{-9}$)</th>
<th>Co-seismic change of volumetric strain ($10^{-9}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2011 $M_w$ 9.1</td>
<td>2.96</td>
<td>1397.16</td>
<td>195.2</td>
</tr>
</tbody>
</table>

subtracting the initial $BK_u$/transmissivity from the average values from the three post-earthquake points within 15 days of the earthquake. Upon calculation, the $BK_u$ values did not change; however, the transmissivity increased obviously after the earthquake, indicating that the low frequency (0.02 Hz) tele-seismic waves hardly had any impact on the variation of the undrained poroelastic parameters of the aquifer. This finding indicates that the tele-seismic waves cannot induce the disruption of the aquifer medium directly; however, they can easily enhance the permeability and induce the transfer of pore pressure in the aquifer. In addition, the co-seismic permeability increased markedly because of the large energy induced by the tele-seismic waves of the 2011 $M_w$ 9.1 Tohoku earthquake.

7. COMPARISON OF VOLUME STRAIN AND WATER LEVEL

Assuming the same $BK_u$ as the initial value for the co-seismic change, we may convert the co-seismic change of water level during the earthquake to the corresponding co-seismic change in volumetric strain with equation (9). The converted value is listed in Table 4. As seen in the table, the converted value shows the same sign as the observed co-seismic change in volumetric strain. The difference (within a ratio factor of 7) between the converted and the observed volumetric strain may be attributed to the unaccounted factors such as ocean tides or energy attenuations.

Finally, to further support the above hypothesis, we compare in Figure 7 the time history of the volumetric strain with that of the water level (pore pressure) in the Fuxin well. In order to facilitate the comparison, we normalize the time series by its maximal value in the first 20 days following the earthquake. Figure 7 shows that the time history of the change in volumetric strain after the earthquake closely resembles that of the change in water level. Furthermore, from Figure 7, we can see that the water level (pore pressure) even changed ahead of the volume strain during the first 5 days after the earthquake. This similarity in change pattern, together...
with the post-seismic similarity between the phase of the tidal response of water level and that in the volumetric strain (Fig. 5), suggests that the co-seismic volumetric strain in the Fuxin well may primarily be produced by the co-seismic change in pore pressure (water level). As discussed above, after the earthquake, the water level may still maintain a dynamic state (i.e. continue to flow into the well or flow out of the well to recover) and influence the volume strain. Meanwhile, the volume strain induced the change of water level in the manner of tidal strain. Thus, during a short time span after the earthquake the phase shifts between the water level and the volume strain approached zero (Fig. 5), thereby indicating that the water level and volumetric strain interacted with each other and changed consistently (Fig. 7).

8. CONCLUSION

In this article, we applied tidal analysis to investigate the volumetric strain and water level documented in the Fuxin well before and after the large \( M_w \) 9.1 Tohoku earthquake. We find that teleseismic waves with a central frequency of 0.02 Hz cannot induce the disruption of the aquifer medium directly, although they can easily enhance the permeability and induce the transfer of pore pressure in the aquifer. Together with the phases, the signs of the co-seismic amplitude change and the co-seismic and post-seismic patterns of volumetric strain and water level, we obtain the coupling mechanism of the volume strain change and the water level change. Before the earthquake, tidal volumetric strain induced the change of water level, that is, the phase of the water level lagged behind that of the volume strain. Moreover, during the earthquake, the permeability enhanced by tele-seismic waves, water level (pore pressure) transferred from high pressure region to the Fuxin well and induced the dilatation of volume strain (phase shifts increased sharply, indicating the change of water level caught up with that of volume strain). Finally, during a short time span after the earthquake, the phase shifts between the water level and the volume strain approached zero, indicating that the water level and volumetric strain interact with each other and change consistently. In addition, we also found that a dynamic energy density of \( \sim 5 \times 10^{-2} \) J/m\(^3\), which resulted from the shaking of the teleseismic waves from the far-field Tohoku earthquake (computed from broadband seismograms), could indirectly generate a dilatation stress of \( \sim 0.0176 \) MPa in the Fuxin well aquifer. Given that the Fuxin well lies in a geothermal area, the results of this study may also have some implications for geothermal resource exploration.

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APPENDIX

![Fig. 1 Lithologic log of the Fuxin well from Seismic monitoring records of China.](image-url)
Fig. 2 Original water level and volume strain at the Fuxin well for the 2011 $M_w$ 9.1 Tohoku earthquake. The vertical dashed lines indicate the start time of the earthquake (Beijing time). (*The coseismic volume strain has been corrected according to the observation records of the Fuxin station).

REFERENCES


Lai, G.J., Ge, H.K., Xue, L., Brodsky, E.E., Huang, F.Q. and Wang, W.W.: 2013, Tidal response variation and recovery following the Wenchuan earthquake from...
water level data of multiple wells in the nearfield. Tectonophysics, 610, 12, 1–12. DOI: 10.1016/j.tecto.2013.08.039


**Fig. 2** (a) Original volume-strain (black thick line), water-level (blue thin line), solid-tide (red thin line), and atmospheric-pressure (black thick line) variations versus time from the Fuxin well before and after the 2011 $M_w$ 9.1 Tohoku earthquake. The arrow indicates the occurrence time of the earthquake; (b) Corrected volume-strain (black thick line) and water-level (blue thin line) variations versus time for the Fuxin well.

**Fig. 3** The spatial distribution of the static volume-strain changes for the 2011 $M_w$ 9.1 Tohoku earthquake, calculated using the elastic half-space dislocation model (Okada, 1992; Lin and Stein, 2004; Toda et al., 2005). Trend, 203°; angle of inclination, 10°; angle of slide, 88°; depth, 20 km; (*Focal Mechanism: Harvard Global CMT) rupture length, 450 km; width, 150 km; and slide range, 2500 cm. The curved solid lines indicate inflation, while the curved dash lines represent compression. The star is the epicenter of the earthquake, the triangles represent the distributed observation stations, the purple lines are the faults, and the bright clear blue lines indicate rivers.

**Fig. 7** Comparison of the first 20 days of the normalized volumetric strain response (black) to the Tohoku earthquake and with the normalized water level (pore pressure) response (red).