

TIME-DEPENDENT MATRIX MULTI-FRACTURE OF SiC/SiC CERAMIC-MATRIX COMPOSITES CONSIDERING INTERFACE OXIDATION

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In this paper, the time-dependent matrix multi-cracking of SiC/SiC ceramic-matrix composites (CMCs) has been investigated considering the fibre/matrix interface oxidation. The time-dependent interface oxidation length and temperature-dependent fibre/matrix interface shear stress in the oxidation and the de-bonded region, the interface de-bonded energy, the fibre and matrix modulus and the matrix fracture energy are considered in the analysis for the micro stress field, the interface debonding criterion and the critical matrix strain energy model. The effects of the fibre volume fraction, the fibre/matrix interface shear stress, the fibre/matrix interface frictional coefficient, the fibre/matrix interface de-bonded energy and the matrix fracture energy on the matrix multi-cracking density and the interface oxidation ratio of SiC/SiC composite are discussed for the different temperatures and oxidation time. The experimental matrix multi-cracking density and fibre/matrix interface oxidation ratio are predicted for unidirectional and mini SiC/SiC composites at different testing temperatures and oxidation time.

INTRODUCTION

Ceramic materials possess high specific strength and a specific modulus at elevated temperatures. But their use as structural components is severely limited due to their brittleness. Continuous fibre-reinforced ceramic-matrix composites (CMCs), by incorporating fibres in the ceramic matrices, not only exploit their attractive high-temperature strength, but also reduce the propensity for catastrophic failure [1, 2, 3]. The environment inside the hot section CMC components is harsh and the composite is typically subjected to complex thermomechanical loading, which can lead to matrix multi-cracking [4, 5]. These matrix cracks form paths for the ingress of the environment oxidising the fibres and leading to a premature failure [6, 7, 8, 9, 10]. The density and openings of these cracks depend on the fibre architecture, the fibre/matrix interface bonding intensity, the applied load and the environments [11, 12, 13]. It is important to develop an understanding of the matrix multi-cracking damage mechanisms at elevated temperatures considering the oxidation damage mechanisms. [14]

Many researchers performed experimental and theoretical investigations on the matrix multi-cracking

evolution of fibre-reinforced CMCs [15, 16, 17, 18, 19, 20, 21]. Morscher et al. [22] established the relationships for the stress-dependent matrix cracking of a 2D SiC/SiC composite, which was related to the stress in the load-bearing SiC matrix. Morscher and Gordon [23] monitored the matrix cracking of a SiC/SiC matrix composite using acoustic emission (AE) and electrical resistance (ER). Racle et al. [24] established the relationship between the characteristic time of a 25 % total fatigue lifetime and the beginning of the matrix cracking using AE. However, in the studies mentioned above, the time-dependent matrix multi-cracking of the SiC/SiC composite at an elevated temperature considering the interface oxidation has not been investigated.

In this paper, the time-dependent matrix multi-cracking of a SiC/SiC composite has been investigated considering the fibre/matrix interface oxidation. The time-dependent interface oxidation length and temperature-dependent fibre/matrix interface shear stress in the oxidation and de-bonded region, the interface de-bonded energy, the fibre and matrix modulus and matrix fracture energy are considered in the analysis for the micro stress field, the interface debonding criterion and the critical matrix strain energy model. The effects of the fibre volume fraction, the fibre/matrix interface shear

stress, the fibre/matrix interface frictional coefficient, the fibre/matrix interface de-bonded energy and the matrix fracture energy on the matrix multi-cracking density and the fibre/matrix interface oxidation ratio of the SiC/SiC composite are discussed for the different temperatures and oxidation time. The experimental matrix multi-cracking density and the fibre/matrix interface oxidation ratio for the unidirectional and mini SiC/SiC composites at different testing temperatures and oxidation time are predicted.

THEORETICAL ANALYSIS

Time-dependent stress analysis

The composite with the fibre volume fraction of V_f is loaded by a remote uniform stress σ normal to the crack plane, as shown in Figure 1. The fibre radius is r_f , and the matrix radius is R ($R = r_f/V_f^{1/2}$). The length of the unit cell is half a matrix crack spacing $l_c/2$, and the interface oxidation length and interface de-bonded length are ζ and l_d , respectively. The time-dependent fibre and matrix axial stress and the fibre/matrix interface shear stress distributions can be determined using the following equations:

$$\sigma_f(z, t, T) = \begin{cases} \frac{\sigma}{V_f} - \frac{2\tau_f(T)}{r_f} z, z \in [0, \zeta(T)] \\ \frac{\sigma}{V_f} - \frac{2\tau_f(T)}{r_f} \zeta(t, T) - \frac{2\tau_i(T)}{r_f} [z - \zeta(t, T)], z \in [\zeta(t, T), l_d(t, T)] \\ \sigma_{fo} + \left[\frac{V_m}{V_f} \sigma_{mo} - \frac{2\tau_f(T)}{r_f} \zeta(t, T) - \frac{2\tau_i(T)}{r_f} [l_d(t, T) - \zeta(t, T)] \right] \\ \times \exp\left[-\rho \frac{z - l_d(t, T)}{r_f}\right], z \in \left[l_d(t, T), \frac{l_c(t, T)}{2}\right] \end{cases} \quad (1)$$

$$\sigma_m(z, t, T) = \begin{cases} 2 \frac{V_f}{V_m} \frac{\tau_f(T)}{r_f} z, z \in [0, \zeta(t, T)] \\ 2 \frac{V_f}{V_m} \frac{\tau_f(T)}{r_f} \zeta(t, T) + 2 \frac{V_f}{V_m} \frac{\tau_i(T)}{r_f} [z - \zeta(t, T)], z \in [\zeta(t, T), l_d(t, T)] \\ \sigma_{mo} + \left[2 \frac{V_f}{V_m} \frac{\tau_f(T)}{r_f} \zeta(t, T) + 2 \frac{V_f}{V_m} \frac{\tau_i(T)}{r_f} [l_d(t, T) - \zeta(t, T)] - \sigma_{mo} \right] \\ \times \exp\left[-\rho \frac{z - l_d(t, T)}{r_f}\right], z \in \left[l_d(t, T), \frac{l_c(t, T)}{2}\right] \end{cases} \quad (2)$$

$$\tau_i(z, t, T) = \begin{cases} \tau_f(T), z \in [0, \zeta(t, T)] \\ \tau_i(T), z \in [\zeta(t, T), l_d(t, T)] \\ \frac{\rho}{2} \left[\frac{V_m}{V_f} \sigma_{mo} - \frac{2\tau_f(T)}{r_f} \zeta(t, T) - \frac{2\tau_i(T)}{r_f} [l_d(t, T) - \zeta(t, T)] \right] \\ \times \exp\left[-\rho \frac{z - l_d(t, T)}{r_f}\right], z \in \left[l_d(t, T), \frac{l_c(t, T)}{2}\right] \end{cases} \quad (3)$$

where

$$\zeta(t, T) = \varphi_1(T) \left[1 - \exp\left(-\frac{\varphi_2(T)t}{b}\right) \right] \quad (4)$$

$$\tau_i(T) = \tau_0 + \mu \frac{|\alpha_{rf}(T) - \alpha_{rm}(T)|(T_m - T)}{A} \quad (5)$$

$$\tau_f(T) = \tau_s + \mu \frac{|\alpha_{rf}(T) - \alpha_{rm}(T)|(T_m - T)}{A} \quad (6)$$

$$\sigma_{fo} = \frac{E_f(T)}{E_c(T)} \sigma + E_f(T)(\alpha_{lc} - \alpha_{lf}) \Delta T \quad (7)$$

$$\sigma_{mo} = \frac{E_m(T)}{E_c(T)} \sigma + E_m(T)(\alpha_{lc} - \alpha_{lm}) \Delta T \quad (8)$$

where $E_f(T)$, $E_m(T)$ and $E_c(T)$ denote the temperature-dependent fibre, matrix and composite elastic modulus, respectively; α_{rf} and α_{rm} denote the fibre and matrix radial thermal expansion coefficient, respectively; α_{lf} , α_{lm} and α_{lc} denote the fibre, matrix and composite axial thermal expansion coefficient, respectively; and ΔT denotes the temperature difference between the fabricated temperature T_0 and the testing temperature T_1 ($\Delta T = T_1 - T_0$).

Time-dependent fibre/matrix interface debonding

The fracture mechanics approach is adopted in the present analysis to determine the fibre/matrix interface de-bonded length. [25]

$$\gamma_d(T) = \frac{F}{4\pi r_f} \frac{\partial w_f(z=0)}{\partial l_d} \frac{1}{2} - \int_0^{l_d(t,T)} \tau_i(T) \frac{\partial v(z)}{\partial l_d} dz \quad (9)$$

where $F(= \pi r_f^2/V_f)$ denotes the fibre load at the matrix cracking plane; $w_f(z=0)$ denotes the fibre axial displacement at the matrix cracking plane and $v(z)$ denotes the relative displacement between the fibre and the matrix. Based on the fibre and matrix axial stress distribution as described in Equations 1 and 2, the fibre and matrix axial displacements of $w_f(z)$ and $w_m(z)$ can be described using the following equations:

$$\begin{aligned} w_f(z) &= \int_z^{\frac{l_c(t,T)}{2}} \frac{\sigma_f(z,t,T)}{E_f(T)} dz \\ &= \frac{\sigma}{V_f E_f(T)} [l_d(t,T) - z] - \frac{\tau_f(T)}{r_f E_f(T)} [2\zeta(t,T)l_d(t,T) - \zeta^2(t,T) - z^2] \\ &\quad - \frac{\tau_i(T)}{r_f E_f(T)} [l_d(t,T) - \zeta(t,T)]^2 + \frac{\sigma_{fo}(T)}{E_f(T)} \left[\frac{l_c(t,T)}{2} - l_d(t,T) \right] \\ &\quad + \frac{r_f}{\rho E_f(T)} \left\{ \frac{V_m}{V_f} \sigma_{mo}(T) - \frac{2\tau_f(T)}{r_f} \zeta(t,T) - \frac{2\tau_i(T)}{r_f} [l_d(t,T) - \zeta(t,T)] \right\} \\ &\quad \times \left\{ 1 - \exp \left[-\rho \frac{l_c(t,T)/2 - l_d(t,T)}{r_f} \right] \right\} \end{aligned} \quad (10)$$

$$\begin{aligned} w_m(z) &= \int_z^{\frac{l_c(t,T)}{2}} \frac{\sigma_m(z,t,T)}{E_m(T)} dz \\ &= \frac{V_f \tau_f(T)}{r_f V_m E_m(T)} [2\zeta(t,T)l_d(t,T) - \zeta^2(t,T) - z^2] \\ &\quad + \frac{V_f \tau_i(T)}{r_f V_m E_m(T)} [l_d(t,T) - \zeta(t,T)]^2 + \frac{\sigma_{mo}(T)}{E_m(T)} \left[\frac{l_c(t,T)}{2} - l_d(t,T) \right] \\ &\quad - \frac{r_f}{\rho E_m(T)} \left\{ \sigma_{mo}(T) - 2 \frac{V_f \tau_f(T)}{r_f V_m} \zeta(t,T) - 2 \frac{V_f \tau_i(T)}{r_f V_m} [l_d(t,T) - \zeta(t,T)] \right\} \\ &\quad \times \left\{ 1 - \exp \left[-\rho \frac{l_c(t,T)/2 - l_d(t,T)}{r_f} \right] \right\} \end{aligned} \quad (11)$$

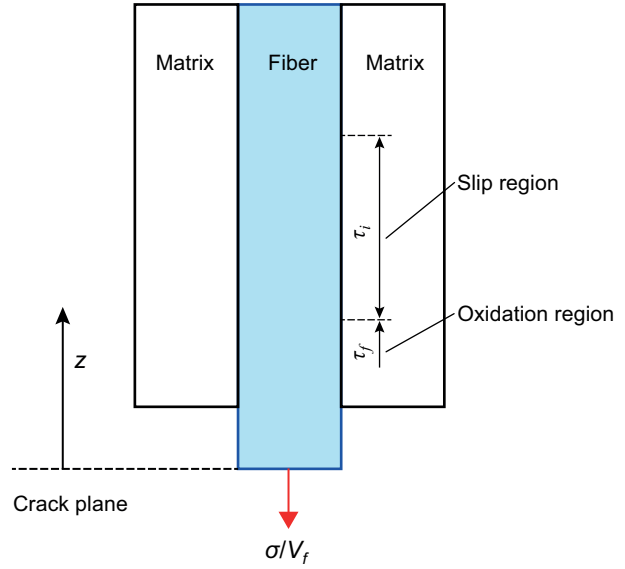


Figure 1. The schematic of the shear-lag model considering the interface oxidation and debonding.

The relative displacement of $v(z)$ between the fibre and the matrix can be described using the following equation:

$$\begin{aligned}
 v(z) &= |w_f(z) - w_m(z)| \\
 &= \frac{\sigma}{V_f E_f(T)} [l_d(t, T) - z] - \frac{E_c(T) \tau_f(T)}{r_f V_m E_m(T) E_f(T)} [2\zeta(t, T) l_d(t, T) - \zeta^2(t, T) - z^2] \\
 &\quad - \frac{E_c(T) \tau_i(T)}{r_f V_m E_m(T) E_f(T)} [l_d(t, T) - \zeta(t, T)]^2 \\
 &\quad + \frac{r_f E_c(T)}{\rho V_m E_m(T) E_f(T)} \left\{ \sigma_{mo}(T) - 2 \frac{\tau_f(T)}{r_f} \zeta(t, T) - 2 \frac{\tau_i(T)}{r_f} [l_d(t, T) - \zeta(t, T)] \right\} \\
 &\quad \times \left\{ 1 - \exp \left[-\rho \frac{l_c(t, T) / 2 - l_d(t, T)}{r_f} \right] \right\}
 \end{aligned} \tag{12}$$

Substituting $w_f(z=0)$ and $v(z)$ into Equation 9, leads to the following equation:

$$\begin{aligned}
 &\frac{E_c(T) \tau_i^2(T)}{r_f V_m E_m(T) E_f(T)} [l_d(t, T) - \zeta(t, T)]^2 + \frac{E_c(T) \tau_i^2(T)}{\rho V_m E_m(T) E_f(T)} [l_d(t, T) - \zeta(t, T)] \\
 &\quad - \frac{\tau_i(T) \sigma}{V_f E_f(T)} [l_d(t, T) - \zeta(t, T)] + \frac{2E_c(T) \tau_f(T) \tau_i(T)}{r_f V_m E_m(T) E_f(T)} \zeta(t, T) [l_d(t, T) - \zeta(t, T)] \\
 &\quad - \frac{r_f \tau_i(T) \sigma}{2\rho V_f E_f(T)} + \frac{E_c(T) \tau_f^2(T)}{r_f V_m E_m(T) E_f(T)} \zeta^2(t, T) + \frac{E_c(T) \tau_f(T) \tau_i(T)}{\rho V_m E_m(T) E_f(T)} \zeta(t, T) \\
 &\quad - \frac{\tau_f(T) \sigma}{V_f E_f(T)} \zeta(t, T) + \frac{r_f V_m E_m(T) \sigma^2}{4V_f^2 E_f(T) E_c(T)} - \gamma_d(T) = 0
 \end{aligned} \tag{13}$$

Solving Equation 13, the fibre/matrix interface de-bonded length can be determined by the following equation:

$$l_d(t, T) = \left[1 - \frac{\tau_f(T)}{\tau_i(T)} \right] \zeta(t, T) + \frac{r_f}{2} \left[\frac{V_m E_m(T) \sigma}{V_f E_c(T) \tau_i(T)} - \frac{1}{\rho} \right] - \sqrt{\left(\frac{r_f}{2\rho} \right)^2 + \frac{r_f V_m E_m(T) E_f(T)}{E_c(T) \tau_i^2(T)} \gamma_d(T)} \tag{14}$$

Time-dependent matrix multi-fracture

The temperature-dependent matrix strain energy can be described using the following equation: [26]

$$U_m(t, T) = \frac{1}{2E_m(T)} \int_{A_m} \int_0^{l_c(T)} \sigma_m^2(z, t, T) dz dA_m \tag{15}$$

where A_m is the cross-section area of the matrix in the unit cell.

When the interface is partially de-bonded, substituting the matrix axial stress in Equation 2 into Equation 15, the matrix strain energy can be described using the following equation:

$$\begin{aligned}
 U_m(t, T) &= \frac{A_m}{E_m} \left\{ \frac{4}{3} \left(\frac{V_f \tau_f(T)}{V_m r_f(T)} \right)^2 \zeta^3(t, T) + 4 \left(\frac{V_f \tau_f(T)}{V_m r_f(T)} \right)^2 [l_d(t, T) - \zeta(t, T)] \zeta^2(t, T) \right. \\
 &\quad + 4 \left(\frac{V_f}{r_f V_m} \right)^2 \tau_f(T) \tau_i(T) \zeta(t, T) [l_d(t, T) - \zeta(t, T)]^2 \\
 &\quad + \frac{4}{3} \left[\frac{V_f \tau_i(T)}{V_m r_f} \right]^2 [l_d(t, T) - \zeta(t, T)]^3 + \sigma_{mo}^2 \left[\frac{l_c(t, T)}{2} - l_d(t, T) \right] \\
 &\quad + \frac{2r_f \sigma_{mo}(T)}{\rho} \left[2 \frac{V_f \tau_f(T)}{V_m r_f} \zeta(t, T) + 2 \frac{V_f \tau_i(T)}{V_m r_f} [l_d(t, T) - \zeta(t, T)] - \sigma_{mo}(T) \right] \\
 &\quad \times \left[1 - \exp \left(-\rho \frac{l_c(t, T) / 2 - l_d(t, T)}{r_f} \right) \right] + \frac{r_f}{2\rho} \left[2 \frac{V_f \tau_f(T)}{V_m r_f} \zeta(t, T) + 2 \frac{V_f \tau_i(T)}{V_m r_f} (l_d(t, T) - \zeta(t, T)) - \sigma_{mo}(T) \right]^2 \\
 &\quad \times \left[1 - \exp \left(-2\rho \frac{l_c(t, T) / 2 - l_d(t, T)}{r_f} \right) \right] \left. \right\}
 \end{aligned} \tag{16}$$

When the interface is completely de-bonded, the matrix strain energy can be described using the following equation:

$$U_m(t, T) = \frac{A_m}{E_m} \left\{ \frac{4}{3} \left[\frac{V_f}{V_m} \frac{\tau_f(T)}{r_f} \right]^2 \zeta^3(t, T) + 4 \left[\frac{V_f}{V_m} \frac{\tau_f(T)}{r_f} \right]^2 \right. \\ \left. [l_d(t, T) - \zeta(t, T)] \zeta^2(t, T) + 4 \left(\frac{V_f}{r_f V_m} \right)^2 \right. \\ \left. \tau_f(T) \tau_i(T) \zeta(t, T) [l_d(t, T) - \zeta(t, T)]^2 \right. \\ \left. + \frac{4}{3} \left[\frac{V_f}{V_m} \frac{\tau_i(T)}{r_f} \right]^2 [l_d(t, T) - \zeta(t, T)]^3 \right\} \quad (17)$$

The critical matrix strain energy of U_{mcr} can be described using the following equation:

$$U_{mcr}(T) = \frac{1}{2} k A_m l_0 \frac{\sigma_{mocr}^2(T)}{E_m(T)} \quad (18)$$

where K ($k \in [0, 1]$) is the critical matrix strain energy parameter; l_0 is the initial matrix crack spacing; and $\sigma_{mocr}(T)$ can be described using the following equation:

$$\sigma_{mocr}(T) = \frac{E_m(T)}{E_c(T)} \sigma_{cr}(T) + E_m(T) [\alpha_{lc}(T) - \alpha_{lm}(T)] \Delta T \quad (19)$$

where $\sigma_{cr}(T)$ denotes the temperature-dependent critical stress corresponding to the composite's proportional limit stress defined by the ACK model: [15]

$$\sigma_{cr}(T) = \left[\frac{6V_f^2 E_f(T) E_c(T) \tau_i(T) \gamma_m(T)}{r_f V_m E_m^2(T)} \right]^{1/3} - \\ - E_c(T) [\alpha_{lc}(T) - \alpha_{lm}(T)] \Delta T \quad (20)$$

where $\gamma_m(T)$ denotes the temperature-dependent matrix fracture energy.

The matrix multi-cracking evolution can be determined using the following equation:

$$U_m(\sigma, t, T) = U_{mcr}(\sigma_{cr}, T) \quad (21)$$

RESULTS AND DISCUSSIONS

The ceramic composite system of SiC/SiC is used for the case study and its material properties are given by: $V_f = 30\%$, $r_f = 7.5 \mu\text{m}$, $E_f = 230 \text{ GPa}$, $\gamma_m = 15 \text{ J}\cdot\text{m}^{-2}$, $\gamma_d = 0.4 \text{ J}\cdot\text{m}^{-2}$, $\tau_0 = 10 \text{ MPa}$, $\alpha_{rf} = 2.9 \times 10^{-6} \text{ K}^{-1}$ and $\alpha_{lf} = 3.9 \times 10^{-6} \text{ K}^{-1}$.

The temperature-dependent SiC matrix elastic modulus of $E_m(T)$ can be described using the following equation: [27]

$$E_m(T) = \frac{350}{460} \left[460 - 0.04T \exp\left(-\frac{962}{T}\right) \right], T \in [300-1773 \text{ K}] \quad (22)$$

The temperature-dependent SiC matrix axial and radial thermal expansion coefficients of $\alpha_{lm}(T)$ and $\alpha_{rm}(T)$ can be described using the following equation, respectively: [27]

$$\alpha_{lm}(T) = \alpha_{rm}(T) = \begin{cases} -1.8276 + 0.0178T - 1.5544 \cdot 10^{-5} T^2 \\ + 4.5246 \cdot 10^{-9} T^3, T \in [125-1273 \text{ K}] \\ 5.0 \cdot 10^{-6} / \text{K}, T > 1273 \text{ K} \end{cases} \quad (23)$$

The temperature dependent fibre/matrix interface de-bonded energy of $\zeta_d(T)$ and the matrix fracture energy of $\zeta_m(T)$ can be described using the following equations, respectively: [28]

$$\gamma_d(T) = \gamma_d^0 \left[1 - \frac{\int_{T_0}^T C_p(T) dT}{\int_{T_0}^{T_m} C_p(T) dT} \right] \quad (24)$$

$$\gamma_m(T) = \gamma_m^0 \left[1 - \frac{\int_{T_0}^T C_p(T) dT}{\int_{T_0}^{T_m} C_p(T) dT} \right] \quad (25)$$

where T_0 denotes the reference temperature; T_m denotes the fabricated temperature; γ_d^0 and γ_m^0 denote the fibre/matrix interface de-bonded energy and the matrix fracture energy at the reference temperature of T_0 ; and $C_p(T)$ can be described using the following equation:

$$C_p(T) = 76.337 + 109.039 \times 10^{-3} T - \\ - 6.535 \times 10^5 T^{-2} - 6.535 \times 10^{-6} T^2 \quad (26)$$

The effects of the fibre volume fraction, the fibre/matrix interface shear stress, the fibre/matrix interface frictional coefficient, the fibre/matrix interface de-bonded energy and the matrix fracture energy on the time-dependent matrix multi-cracking density and the interface oxidation ratio are discussed.

Effect of the fibre volume fraction

The effect of the fibre volume fraction (i.e., $V_f = 25\%$, 30% and 35%) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation ratio of the SiC/SiC composite at $T = 873 \text{ K}$, 973 K and 1073 K for the oxidation time of $t = 1 \text{ h}$ and 3 h are shown in Figure 2.

When $V_f = 25\%$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\phi = 1.2/\text{mm}$ at $\sigma_{cr} = 110 \text{ MPa}$ to $\phi = 11.9/\text{mm}$ at $\sigma_{sat} = 120 \text{ MPa}$, and the fibre/matrix interface oxidation ratio decreases from $\zeta/l_d = 6\%$ to $\zeta/l_d = 3.4\%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\phi = 0.67 \text{ mm}$ at $\sigma_{cr} = 110 \text{ MPa}$ to $\phi = 10.7/\text{mm}$ at $\sigma_{sat} = 123 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 16.6\%$ to $\zeta/l_d = 9.8\%$. At $T = 973 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\phi = 0.24/\text{mm}$ at $\sigma_{cr} = 104 \text{ MPa}$ to $\phi = 9.2/\text{mm}$ at $\sigma_{sat} = 133 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 16.7\%$ to $\zeta/l_d = 9.5\%$; and at

$t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.17/\text{mm}$ at $\sigma_{\text{cr}} = 104$ MPa to $\varphi = 7.4/\text{mm}$ at $\sigma_{\text{sat}} = 140$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 40.5\%$ to $\zeta/l_d = 25.1\%$. At $T = 1073$ K and

$t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 96$ MPa to $\varphi = 7/\text{mm}$ at $\sigma_{\text{sat}} = 144$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 6.7\%$ to $\zeta/l_d = 21.1\%$; and at $t = 3$ h, the matrix multi-

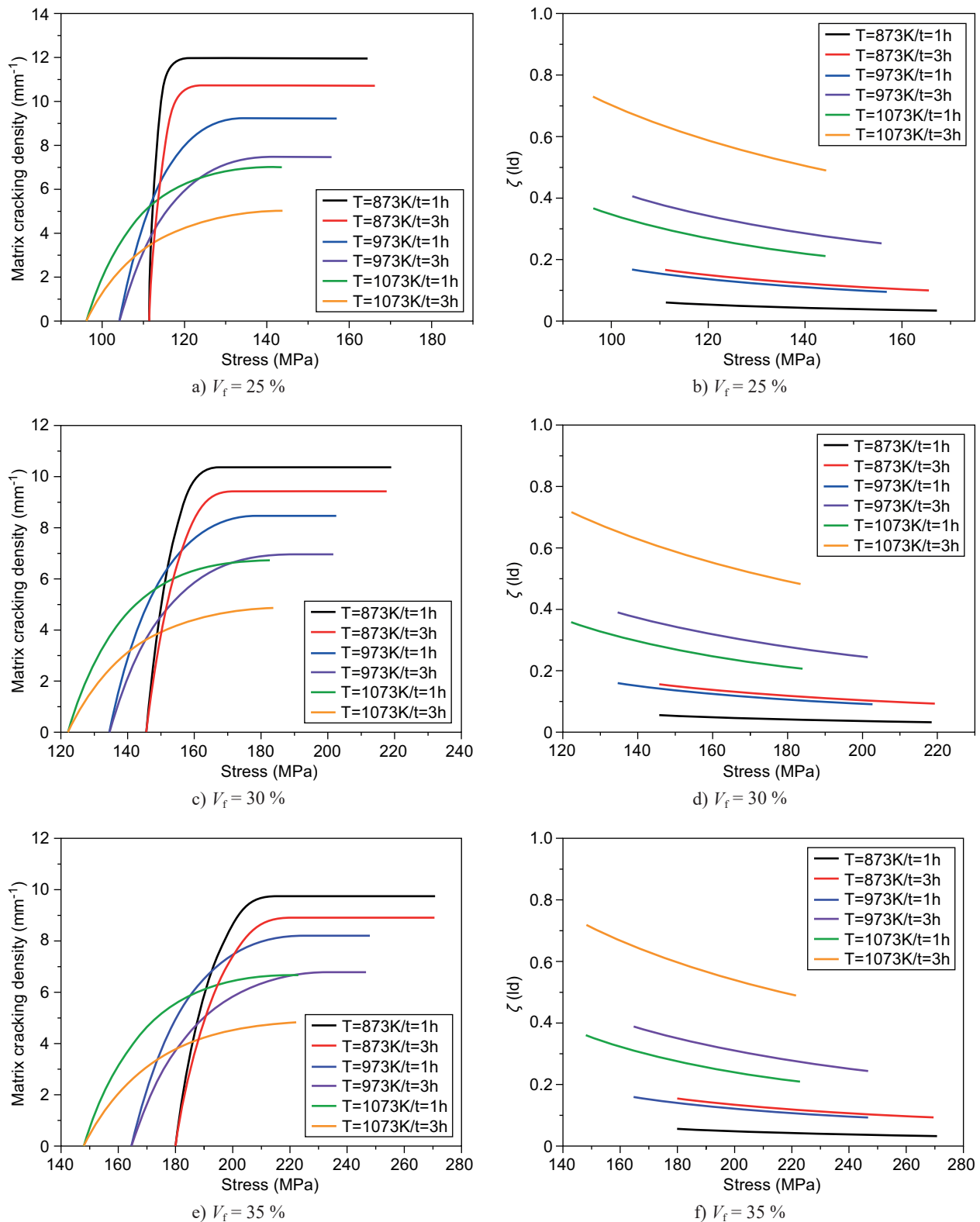


Figure 2. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $V_f = 25\%$ (a), 30% (c), 35% (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $V_f = 25\%$ (b), 30% (d), 35% (f).

cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 96.3 \text{ MPa}$ to $\varphi = 5.0/\text{mm}$ at $\sigma_{\text{sat}} = 144 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 72.8 \%$ to $\zeta/l_d = 48.9 \%$.

When $V_f = 30 \%$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.47/\text{mm}$ at $\sigma_{\text{cr}} = 146 \text{ MPa}$ to $\varphi = 10.36/\text{mm}$ at $\sigma_{\text{sat}} = 167 \text{ MPa}$, and the fibre/matrix interface oxidation ratio decreases from $\zeta/l_d = 5.6 \%$ to $\zeta/l_d = 3.2 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{\text{cr}} = 146 \text{ MPa}$ to $\varphi = 3.4/\text{mm}$ at $\sigma_{\text{sat}} = 170 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 15.6 \%$ to $\zeta/l_d = 9.3 \%$. At $T = 973 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{\text{cr}} = 134 \text{ MPa}$ to $\varphi = 8.46/\text{mm}$ at $\sigma_{\text{sat}} = 178 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 15.9 \%$ to $\zeta/l_d = 9.1 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 134 \text{ MPa}$ to $\varphi = 6.9/\text{mm}$ at $\sigma_{\text{sat}} = 186 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 38.9 \%$ to $\zeta/l_d = 24.3 \%$. At $T = 1073 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{\text{cr}} = 122 \text{ MPa}$ to $\varphi = 6.7/\text{mm}$ at $\sigma_{\text{sat}} = 183 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 35.7 \%$ to $\zeta/l_d = 20.7 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 122 \text{ MPa}$ to $\varphi = 4.8/\text{mm}$ at $\sigma_{\text{sat}} = 183 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 71.5 \%$ to $\zeta/l_d = 48.2 \%$.

When $V_f = 35 \%$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{\text{cr}} = 180 \text{ MPa}$ to $\varphi = 9.75/\text{mm}$ at $\sigma_{\text{sat}} = 215 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 5.5 \%$ to $\zeta/l_d = 3.2 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.28/\text{mm}$ at $\sigma_{\text{cr}} = 180 \text{ MPa}$ to $\varphi = 8.9/\text{mm}$ at $\sigma_{\text{sat}} = 219 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 15.4 \%$ to 9.2% . At $T = 973 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{\text{cr}} = 165 \text{ MPa}$ to $\varphi = 8.2/\text{mm}$ at $\sigma_{\text{sat}} = 223 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 15.9 \%$ to $\zeta/l_d = 9.2 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 165 \text{ MPa}$ to $\varphi = 6.7/\text{mm}$ at $\sigma_{\text{sat}} = 234 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 38.8 \%$ to $\zeta/l_d = 24.3 \%$. At $T = 1073 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{\text{cr}} = 148 \text{ MPa}$ to $\varphi = 6.6/\text{mm}$ at $\sigma_{\text{sat}} = 222 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 36 \%$ to $\zeta/l_d = 21 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 148 \text{ MPa}$ to $\varphi = 4.8/\text{mm}$ at $\sigma_{\text{sat}} = 222 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 71.9 \%$ to 48.7% .

Effect of the fibre/matrix interface shear stress

The effect of interface shear stress (i.e., $\tau_0 = 15, 20$ and 25 MPa) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation ratio of

the SiC/SiC composite at $T = 873 \text{ K}, 973 \text{ K}$ and 1073 K for $t = 1 \text{ h}$ and 3 h are shown in Figure 3.

When $\tau_0 = 15 \text{ MPa}$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.34/\text{mm}$ at $\sigma_{\text{cr}} = 191 \text{ MPa}$ to $\varphi = 10.33/\text{mm}$ at $\sigma_{\text{sat}} = 234 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 6 \%$ to $\zeta/l_d = 3.5 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.27/\text{mm}$ at $\sigma_{\text{cr}} = 191 \text{ MPa}$ to $\varphi = 9.3/\text{mm}$ at $\sigma_{\text{sat}} = 240 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 16.6 \%$ to $\zeta/l_d = 10.2 \%$. At $T = 973 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{\text{cr}} = 176 \text{ MPa}$ to $\varphi = 8.7/\text{mm}$ at $\sigma_{\text{sat}} = 245 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 17.1 \%$ to $\zeta/l_d = 10.1 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 176 \text{ MPa}$ to $\varphi = 7/\text{mm}$ at $\sigma_{\text{sat}} = 258 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 40.6 \%$ to $\zeta/l_d = 26.3 \%$. At $T = 1073 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 159 \text{ MPa}$ to $\varphi = 7/\text{mm}$ at $\sigma_{\text{sat}} = 239 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 37.5 \%$ to $\zeta/l_d = 22.8 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 159 \text{ MPa}$ to $\varphi = 4.8/\text{mm}$ at $\sigma_{\text{sat}} = 239 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 71.7 \%$ to $\zeta/l_d = 50.9 \%$.

When $\tau_0 = 20 \text{ MPa}$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.34/\text{mm}$ at $\sigma_{\text{cr}} = 201 \text{ MPa}$ to $\varphi = 10.89/\text{mm}$ at $\sigma_{\text{sat}} = 251 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 6.5 \%$ to $\zeta/l_d = 3.9 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.27/\text{mm}$ at $\sigma_{\text{cr}} = 201 \text{ MPa}$ to $\varphi = 9.7/\text{mm}$ at $\sigma_{\text{sat}} = 260 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 17.7 \%$ to $\zeta/l_d = 11 \%$. At $T = 973 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.22/\text{mm}$ at $\sigma_{\text{cr}} = 186 \text{ MPa}$ to $\varphi = 9.26/\text{mm}$ at $\sigma_{\text{sat}} = 265 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 18.2 \%$ to $\zeta/l_d = 11 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 186 \text{ MPa}$ to $\varphi = 7.3/\text{mm}$ at $\sigma_{\text{sat}} = 280 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 42.3 \%$ to $\zeta/l_d = 28.1 \%$. At $T = 1073 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 169 \text{ MPa}$ to $\varphi = 7.4/\text{mm}$ at $\sigma_{\text{sat}} = 254 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 39 \%$ to $\zeta/l_d = 24.5 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 169 \text{ MPa}$ to $\varphi = 4.9/\text{mm}$ at $\sigma_{\text{sat}} = 254 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 72.1 \%$ to $\zeta/l_d = 52.9 \%$.

When $\tau_0 = 25 \text{ MPa}$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{\text{cr}} = 211 \text{ MPa}$ to $\varphi = 11.4/\text{mm}$ at $\sigma_{\text{sat}} = 270 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 7 \%$ to $\zeta/l_d = 4.2 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.28/\text{mm}$ at $\sigma_{\text{cr}} = 211 \text{ MPa}$ to $\varphi = 10.2/\text{mm}$ at $\sigma_{\text{sat}} = 277 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 18.8 \%$ to $\zeta/l_d = 11.8 \%$.

At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.23/\text{mm}$ at $\sigma_{\text{cr}} = 195$ MPa to $\varphi = 9.7/\text{mm}$ at $\sigma_{\text{sat}} = 282$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 19.3\%$ to $\zeta/l_d = 11.8\%$;

and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 195$ MPa to $\varphi = 7.5/\text{mm}$ at $\sigma_{\text{sat}} = 293$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 43.8\%$ to $\zeta/l_d = 29.7\%$. At $T = 1073$ K

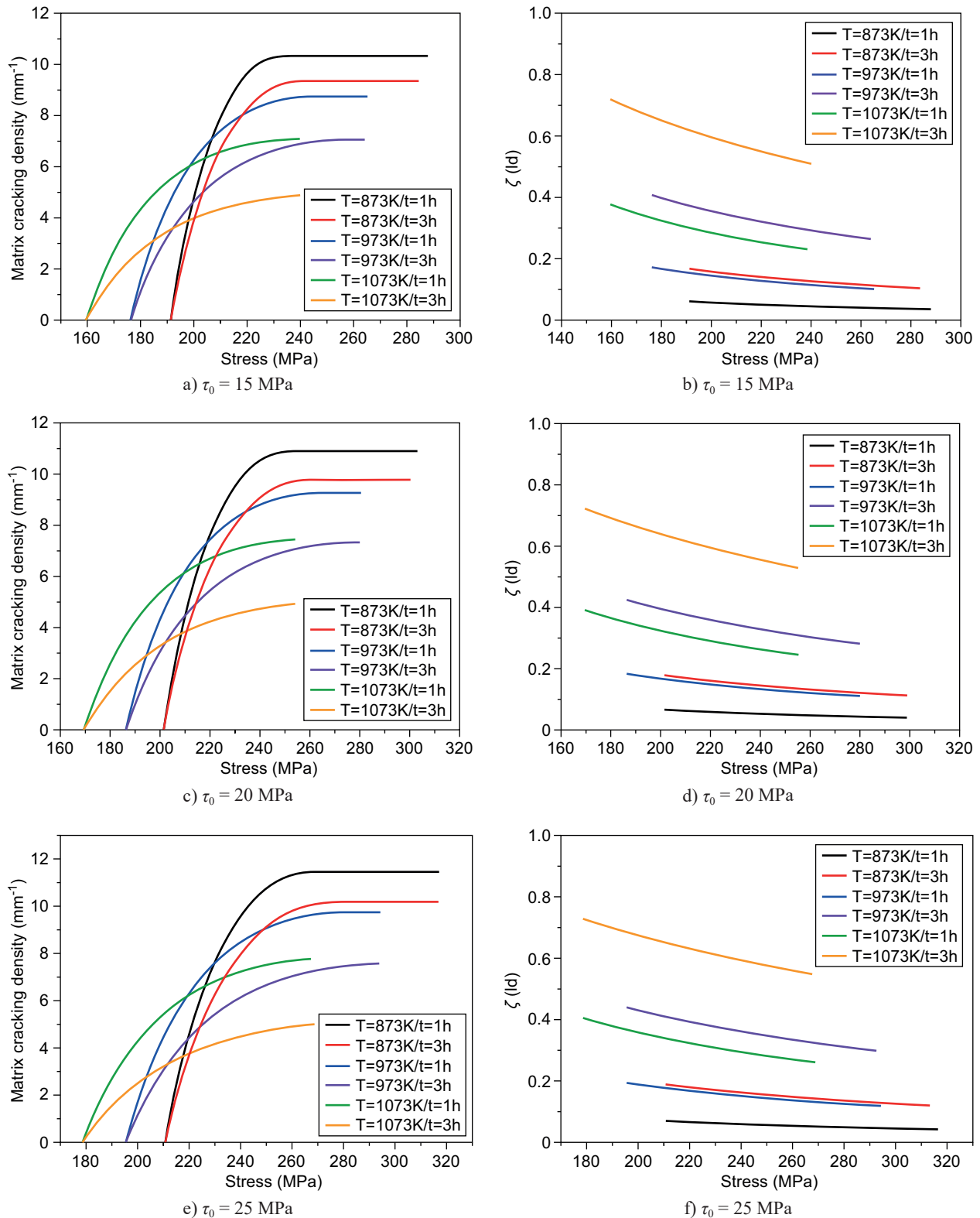


Figure 3. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $\tau_0 = 15$ MPa (a), 20 MPa (c), 25 MPa (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $\tau_0 = 15$ MPa (b), 20 MPa (d), 25 MPa (f).

and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.16/\text{mm}$ at $\sigma_{\text{cr}} = 178$ MPa to $\varphi = 7.7/\text{mm}$ at $\sigma_{\text{sat}} = 268$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 40.4\%$ to $\zeta/l_d = 26.1\%$; and at $t = 3$ h, the ma-

trix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{\text{cr}} = 178$ MPa to $\varphi = 5/\text{mm}$ at $\sigma_{\text{sat}} = 268$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 72.6\%$ to $\zeta/l_d = 54.6\%$.

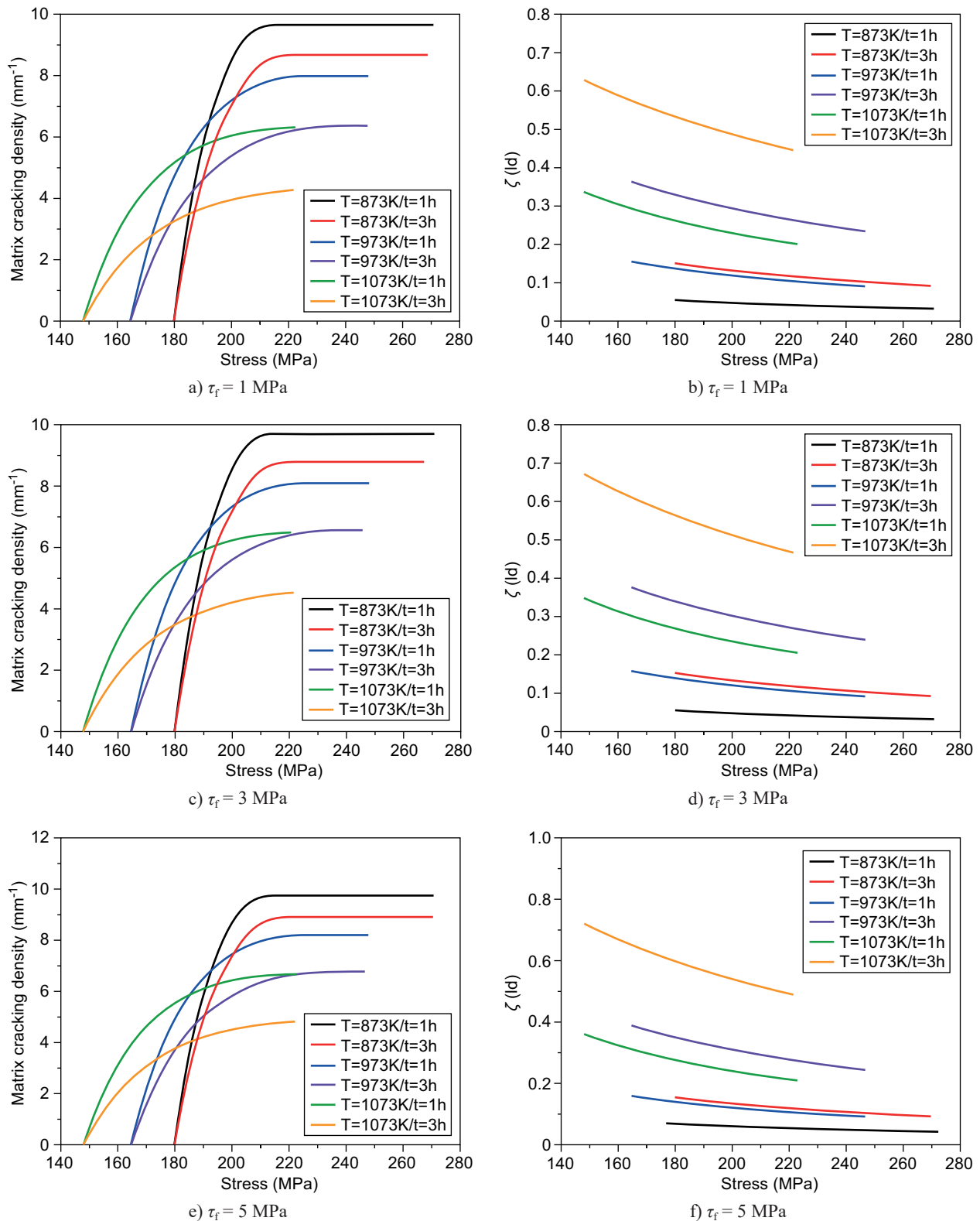


Figure 4. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $\tau_f = 1$ MPa (a), 3 MPa (c), 5 MPa (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $\tau_f = 1$ MPa (b), 3 MPa (d), 5 MPa (f).

The effect of interface shear stress (i.e., $\tau_f = 1, 3$ and 5 MPa) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation of the SiC/SiC composite at $T = 873$ K, 973 K and 1073 K for $t = 1$ h and 3 h are shown in Figure 4.

When $\tau_f = 1$ MPa at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.34/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 9.6/\text{mm}$ at $\sigma_{sat} = 214$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.5\%$ to $\zeta/l_d = 3.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.27/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 8.6/\text{mm}$ at $\sigma_{sat} = 220$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15\%$ to $\zeta/l_d = 9.1\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.19/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 7.9/\text{mm}$ at $\sigma_{sat} = 225$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15.4\%$ to $\zeta/l_d = 9\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.13/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 6.3/\text{mm}$ at $\sigma_{sat} = 237$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 36.2\%$ to $\zeta/l_d = 23.3\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.13/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 6.3/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 33.5\%$ to $\zeta/l_d = 20\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.07/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 4.2/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 62.7\%$ to $\zeta/l_d = 44.3\%$.

When $\tau_f = 3$ MPa at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 9.7/\text{mm}$ at $\sigma_{sat} = 214$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.5\%$ to $\zeta/l_d = 3.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.28/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 8.7/\text{mm}$ at $\sigma_{sat} = 220$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15.2\%$ to $\zeta/l_d = 9.2\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 8.0/\text{mm}$ at $\sigma_{sat} = 224$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15.6\%$ to $\zeta/l_d = 9.1\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 6.5/\text{mm}$ at $\sigma_{sat} = 236$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 37.5\%$ to $\zeta/l_d = 23.8\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 6.4/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 34.7\%$ to $\zeta/l_d = 20.5\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.08/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 4.5/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 67\%$ to $\zeta/l_d = 46.4\%$.

When $\tau_f = 5$ MPa at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 9.7/\text{mm}$ at $\sigma_{sat} = 214$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.5\%$ to

$\zeta/l_d = 3.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.29/\text{mm}$ at $\sigma_{cr} = 180$ MPa to $\varphi = 8.9/\text{mm}$ at $\sigma_{sat} = 220$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15.4\%$ to $\zeta/l_d = 9.3\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 8.2/\text{mm}$ at $\sigma_{sat} = 224$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 15.9\%$ to $\zeta/l_d = 9.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 165$ MPa to $\varphi = 6.7/\text{mm}$ at $\sigma_{sat} = 234$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 38.8\%$ to $\zeta/l_d = 24.3\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 6.6/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 36\%$ to $\zeta/l_d = 21\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 148$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 72\%$ to $\zeta/l_d = 48.7\%$.

Effect of the fibre/matrix interface frictional coefficient

The effect of the fibre/matrix interface frictional coefficient (i.e., $\mu = 0.05, 0.1$ and 0.15) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation ratio of the SiC/SiC composite at $T = 873$ K, 973 K and 1073 K for $t = 1$ h and 3 h are shown in Figure 5.

When $\mu = 0.05$ at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 1.2/\text{mm}$ at $\sigma_{cr} = 128$ MPa to $\varphi = 9.9/\text{mm}$ at $\sigma_{sat} = 136$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 4.9\%$ to $\zeta/l_d = 2.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.71/\text{mm}$ at $\sigma_{cr} = 128$ MPa to $\varphi = 9.2/\text{mm}$ at $\sigma_{sat} = 138$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 13.8\%$ to $\zeta/l_d = 7.9\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{cr} = 120$ MPa to $\varphi = 7.9/\text{mm}$ at $\sigma_{sat} = 151$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 14.5\%$ to $\zeta/l_d = 7.9\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.16/\text{mm}$ at $\sigma_{cr} = 120$ MPa to $\varphi = 6.7/\text{mm}$ at $\sigma_{sat} = 156$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 37.1\%$ to $\zeta/l_d = 21.7\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{cr} = 110$ MPa to $\varphi = 6.3/\text{mm}$ at $\sigma_{sat} = 162$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 34.8\%$ to $\zeta/l_d = 18.8\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 110$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 166$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 73.7\%$ to $\zeta/l_d = 46.1\%$.

When $\mu = 0.1$ at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.47/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 10.3/\text{mm}$ at $\sigma_{sat} = 167$ MPa, and the

interface oxidation ratio decreases from $\zeta/l_d = 5.6\%$ to $\zeta/l_d = 3.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{sat} = 170$ MPa, and the interface oxida-

tion ratio decreases from $\zeta/l_d = 15.6\%$ to $\zeta/l_d = 9.3\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 8.4/\text{mm}$ at $\sigma_{sat} = 178$ MPa, and the interface oxidation

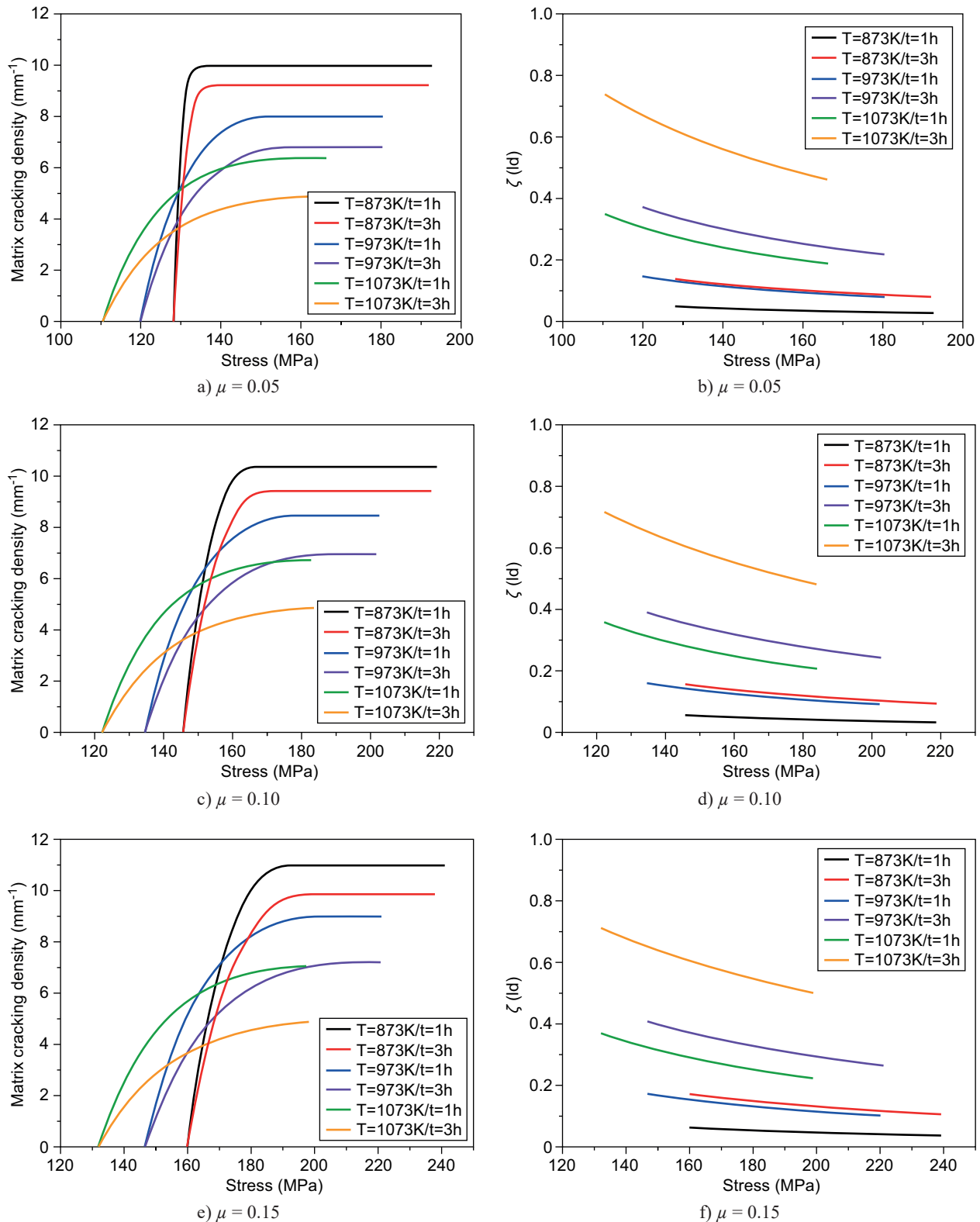


Figure 5. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $\mu = 0.05$ (a), 0.10 (c), 0.15 (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $\mu = 0.05$ (b), 0.10 (d), 0.15 (f).

ratio decreases from $\zeta/l_d = 15.9\%$ to $\zeta/l_d = 9.1\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 6.9/\text{mm}$ at $\sigma_{sat} = 186$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 38.9\%$ to $\zeta/l_d = 24.3\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 6.7/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 35.7\%$ to $\zeta/l_d = 20.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 71.5\%$ to $\zeta/l_d = 48.2\%$.

When $\mu = 0.15$ at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.4/\text{mm}$ at $\sigma_{cr} = 160$ MPa to $\varphi = 10.9/\text{mm}$ at $\sigma_{sat} = 193$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 6.3\%$ to $\zeta/l_d = 3.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.31/\text{mm}$ at $\sigma_{cr} = 160$ MPa to $\varphi = 9.8/\text{mm}$ at $\sigma_{sat} = 198$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 17.1\%$ to $\zeta/l_d = 10.5\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.22/\text{mm}$ at $\sigma_{cr} = 147$ MPa to $\varphi = 8.9/\text{mm}$ at $\sigma_{sat} = 201$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 17.2\%$ to $\zeta/l_d = 10.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 147$ MPa to $\varphi = 7.2/\text{mm}$ at $\sigma_{sat} = 212$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 40.7\%$ to $\zeta/l_d = 26.5\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 132$ MPa to $\varphi = 7/\text{mm}$ at $\sigma_{sat} = 198$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 36.9\%$ to $\zeta/l_d = 22.4\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 132$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 198$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 71\%$ to $\zeta/l_d = 50.1\%$.

Effect of the fibre/matrix interface de-bonded energy

The effect of the fibre/matrix interface de-bonded energy (i.e., $\gamma_d = 0.3, 0.5$ and 0.7 J·m⁻²) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation ratio of the SiC/SiC composite at $T = 873$ K, 973 K and 1073 K for $t = 1$ h and 3 h are shown in Figure 6.

When $\gamma_d = 0.3$ J·m⁻² at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.7/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 10.3/\text{mm}$ at $\sigma_{sat} = 160$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.2\%$ to $\zeta/l_d = 3.1\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.49/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{sat} = 164$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 14.7\%$ to $\zeta/l_d = 9.0\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking

density increases from $\varphi = 0.24/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 8.4/\text{mm}$ at $\sigma_{sat} = 171$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 14.7\%$ to $\zeta/l_d = 8.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.16/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 6.9/\text{mm}$ at $\sigma_{sat} = 179$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 36.5\%$ to $\zeta/l_d = 23.3\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 6.7/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 32.6\%$ to $\zeta/l_d = 19.6\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 67.3\%$ to $\zeta/l_d = 46.3\%$.

When $\gamma_d = 0.5$ J·m⁻² at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.3/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 10.3/\text{mm}$ at $\sigma_{sat} = 173$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.9\%$ to $\zeta/l_d = 3.3\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.29/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{sat} = 176$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 16.5\%$ to $\zeta/l_d = 9.6\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 8.4/\text{mm}$ at $\sigma_{sat} = 184$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 17.1\%$ to $\zeta/l_d = 9.5\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 6.9/\text{mm}$ at $\sigma_{sat} = 192$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 41.2\%$ to $\zeta/l_d = 25.2\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 6.7/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 38.9\%$ to $\zeta/l_d = 21.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$ at $\sigma_{cr} = 122$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 75.6\%$ to $\zeta/l_d = 50\%$.

When $\gamma_d = 0.7$ J·m⁻² at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.3/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 10.3/\text{mm}$ at $\sigma_{sat} = 183$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 6.7\%$ to $\zeta/l_d = 3.6\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.24/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{sat} = 186$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 18.2\%$ to $\zeta/l_d = 10.2\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 8.4/\text{mm}$ at $\sigma_{sat} = 202$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 19.7\%$ to $\zeta/l_d = 10.3\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 134$ MPa to $\varphi = 6.9/\text{mm}$ at $\sigma_{sat} = 202$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 46\%$ to $\zeta/l_d = 27\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from

$\varphi = 0.16/\text{mm}$ at $\sigma_{\text{cr}} = 122 \text{ MPa}$ to $\varphi = 6.8/\text{mm}$ at $\sigma_{\text{sat}} = 183 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 46 \%$ to $\zeta/l_d = 23.8 \%$; and at $t = 3 \text{ h}$, the matrix multi-cracking density increases from $\varphi = 0.09/\text{mm}$

at $\sigma_{\text{cr}} = 122 \text{ MPa}$ to $\varphi = 4.9/\text{mm}$ at $\sigma_{\text{sat}} = 183 \text{ MPa}$, and the interface oxidation ratio decreases from $\zeta/l_d = 84.1 \%$ to $\zeta/l_d = 53.6 \%$.

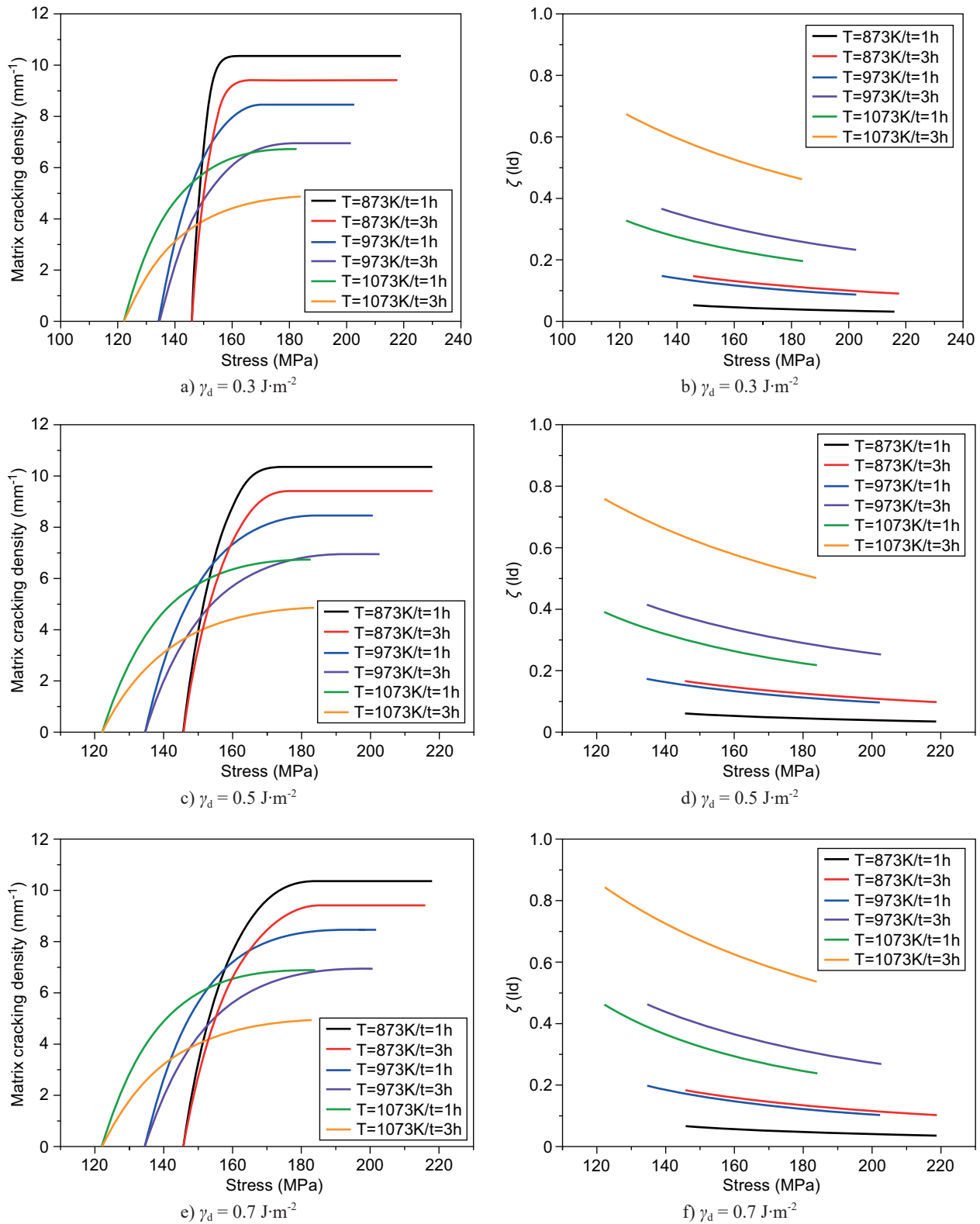


Figure 6. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $\gamma_d = 0.3 \text{ J} \cdot \text{m}^{-2}$ (a), $0.5 \text{ J} \cdot \text{m}^{-2}$ (c), $0.7 \text{ J} \cdot \text{m}^{-2}$ (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $\gamma_d = 0.3 \text{ J} \cdot \text{m}^{-2}$ (b), $0.5 \text{ J} \cdot \text{m}^{-2}$ (d), $0.7 \text{ J} \cdot \text{m}^{-2}$ (f).

Effect of the matrix fracture energy

The effect of the matrix fracture energy (i.e., $\gamma_m = 20$, 25 and $30 \text{ J}\cdot\text{m}^{-2}$) on the time-dependent matrix multi-cracking and the fibre/matrix interface oxidation ratio of

the SiC/SiC composite at $T = 873 \text{ K}$, 973 K and 1073 K for $t = 1 \text{ h}$ and 3 h are shown in Figure 7.

When $\gamma_m = 20 \text{ J}\cdot\text{m}^{-2}$ at $T = 873 \text{ K}$ and $t = 1 \text{ h}$, the matrix multi-cracking density increases from $\rho = 0.3/\text{mm}$

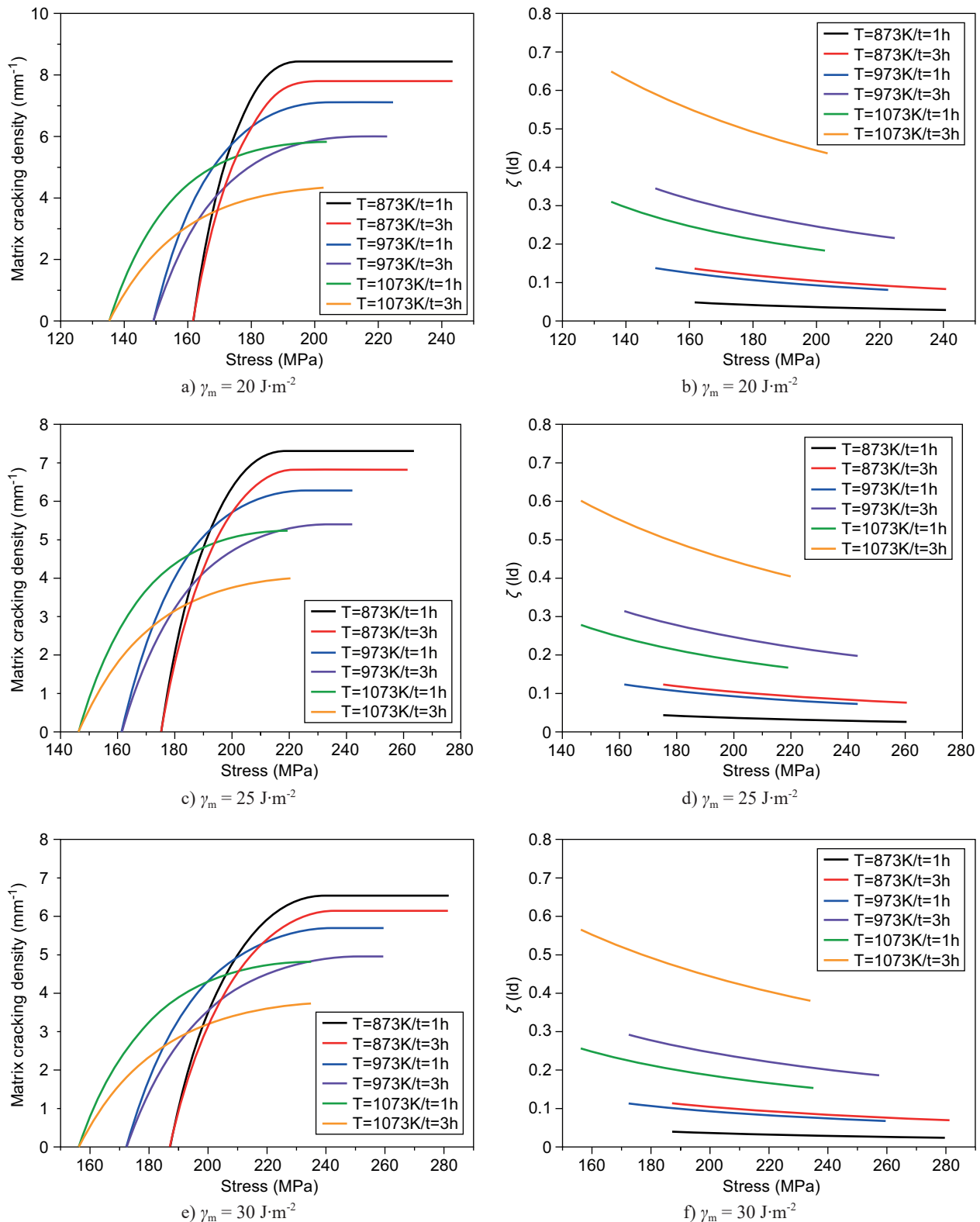


Figure 7. The matrix cracking density versus the applied stress curves for the different oxidation temperature and time when $\gamma_m = 20 \text{ J}\cdot\text{m}^{-2}$ (a), $25 \text{ J}\cdot\text{m}^{-2}$ (c), $30 \text{ J}\cdot\text{m}^{-2}$ (e); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time when $\gamma_m = 20 \text{ J}\cdot\text{m}^{-2}$ (b), $25 \text{ J}\cdot\text{m}^{-2}$ (d), $30 \text{ J}\cdot\text{m}^{-2}$ (f).

at $\sigma_{cr} = 162$ MPa to $\varphi = 8.4/\text{mm}$ at $\sigma_{sat} = 195$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 4.8\%$ to $\zeta/l_d = 2.8\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.24/\text{mm}$ at $\sigma_{cr} = 162$ MPa to $\varphi = 7.8/\text{mm}$ at $\sigma_{sat} = 199$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 13.6\%$ to $\zeta/l_d = 8.2\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.18/\text{mm}$ at $\sigma_{cr} = 149$ MPa to $\varphi = 7.1/\text{mm}$ at $\sigma_{sat} = 204$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 13.7\%$ to $\zeta/l_d = 8\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.13/\text{mm}$ at $\sigma_{cr} = 149$ MPa to $\varphi = 6/\text{mm}$ at $\sigma_{sat} = 212$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 34.4\%$ to $\zeta/l_d = 21.6\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.13/\text{mm}$ at $\sigma_{cr} = 135$ MPa to $\varphi = 5.8/\text{mm}$ at $\sigma_{sat} = 203$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 30.9\%$ to $\zeta/l_d = 18.2\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.08/\text{mm}$ at $\sigma_{cr} = 135$ MPa to $\varphi = 4.3/\text{mm}$ at $\sigma_{sat} = 203$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 64.7\%$ to $\zeta/l_d = 43.6\%$.

When $\gamma_m = 25 \text{ J}\cdot\text{m}^{-2}$ at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.23/\text{mm}$ at $\sigma_{cr} = 175$ MPa to $\varphi = 7.3/\text{mm}$ at $\sigma_{sat} = 218$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 4.3\%$ to $\zeta/l_d = 2.6\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 175$ MPa to $\varphi = 6.8/\text{mm}$ at $\sigma_{sat} = 222$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 12.2\%$ to $\zeta/l_d = 7.5\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{cr} = 162$ MPa to $\varphi = 6.2/\text{mm}$ at $\sigma_{sat} = 243$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 12.3\%$ to $\zeta/l_d = 7.3\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.12/\text{mm}$ at $\sigma_{cr} = 162$ MPa to $\varphi = 5.4/\text{mm}$ at $\sigma_{sat} = 234$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 31.3\%$ to $\zeta/l_d = 19.8\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.12/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 5.2/\text{mm}$ at $\sigma_{sat} = 220$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 27.7\%$ to $\zeta/l_d = 16.5\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.08/\text{mm}$ at $\sigma_{cr} = 146$ MPa to $\varphi = 4.0/\text{mm}$ at $\sigma_{sat} = 220$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 60\%$ to $\zeta/l_d = 40.4\%$.

When $\gamma_m = 30 \text{ J}\cdot\text{m}^{-2}$ at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{cr} = 187$ MPa to $\varphi = 6.5/\text{mm}$ at $\sigma_{sat} = 239$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 4\%$ to $\zeta/l_d = 2.4\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.17/\text{mm}$ at $\sigma_{cr} = 167$ MPa to $\varphi = 6.1/\text{mm}$ at $\sigma_{sat} = 242$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 11.3\%$ to $\zeta/l_d = 6.9\%$. At $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.14/\text{mm}$ at $\sigma_{cr} = 172$ MPa to

$\varphi = 5.6/\text{mm}$ at $\sigma_{sat} = 243$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 11.2\%$ to $\zeta/l_d = 6.7\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.11/\text{mm}$ at $\sigma_{cr} = 172$ MPa to $\varphi = 4.9/\text{mm}$ at $\sigma_{sat} = 253$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 29.1\%$ to $\zeta/l_d = 18.4\%$. At $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.11/\text{mm}$ at $\sigma_{cr} = 156$ MPa to $\varphi = 4.8/\text{mm}$ at $\sigma_{sat} = 234$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 25.4\%$ to $\zeta/l_d = 15.3\%$; and at $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.07/\text{mm}$ at $\sigma_{cr} = 156$ MPa to $\varphi = 3.7/\text{mm}$ at $\sigma_{sat} = 234$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 56.3\%$ to $\zeta/l_d = 37.9\%$.

EXPERIMENTAL COMPARISONS

The experimental and theoretical matrix multi-cracking density and the fibre/matrix interface oxidation ratio of the unidirectional SiC/SiC [29] and mini SiC/SiC [30] composites composite at room temperature, $T = 773$ K, 873 K, 973 K and 1073 K for $t = 1$ h and 3 h are predicted, as shown in Figures 8 and 9.

The unidirectional SiC/SiC composite

Beyerle et al. [29] investigated the damage evolution of the matrix multi-cracking in the unidirectional SiC/SiC composite. At room temperature, the matrix multi-cracking evolution starts at $\sigma_{cr} = 240$ MPa and approaches saturation at $\sigma_{sat} = 320$ MPa; and the matrix cracking density increases from $\varphi = 1.1/\text{mm}$ to $\varphi = 13/\text{mm}$.

At $T = 773$ K, the matrix multi-cracking density increases from $\varphi = 0.5/\text{mm}$ at $\sigma_{cr} = 222$ MPa to $\varphi = 12.4/\text{mm}$ at $\sigma_{sat} = 311$ MPa; at $T = 773$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.36/\text{mm}$ at $\sigma_{cr} = 222$ MPa to $\varphi = 11.9/\text{mm}$ at $\sigma_{sat} = 272$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 2\%$ at $\sigma_{cr} = 222$ MPa to $\zeta/l_d = 1.1\%$ at $\sigma_{sat} = 272$ MPa; and at $T = 773$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.34/\text{mm}$ at $\sigma_{cr} = 222$ MPa to $\varphi = 11.5/\text{mm}$ at $\sigma_{sat} = 273$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 5.8\%$ at $\sigma_{cr} = 222$ MPa to $\zeta/l_d = 3.4\%$ at $\sigma_{sat} = 273$ MPa.

At $T = 873$ K, the matrix multi-cracking density increases from $\varphi = 0.45/\text{mm}$ at $\sigma_{cr} = 206$ MPa to $\varphi = 11.2/\text{mm}$ at $\sigma_{sat} = 288$ MPa; at $T = 873$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.25/\text{mm}$ at $\sigma_{cr} = 206$ MPa to $\varphi = 10.3/\text{mm}$ at $\sigma_{sat} = 288$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 8.3\%$ at $\sigma_{cr} = 206$ MPa to $\zeta/l_d = 4.6\%$ at $\sigma_{sat} = 288$ MPa; and at $T = 873$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{cr} = 206$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{sat} = 288$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 22.3\%$ at $\sigma_{cr} = 206$ MPa to $\zeta/l_d = 13\%$ at $\sigma_{sat} = 288$ MPa.

At $T = 973$ K, the matrix multi-cracking density increases from $\varphi = 0.4/\text{mm}$ at $\sigma_{\text{cr}} = 188$ MPa to $\varphi = 10.2/\text{mm}$ at $\sigma_{\text{sat}} = 263$ MPa; at $T = 973$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.21/\text{mm}$ at $\sigma_{\text{cr}} = 188$ MPa to $\varphi = 8.8/\text{mm}$ at $\sigma_{\text{sat}} = 263$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 26.3$ % at $\sigma_{\text{cr}} = 188$ MPa to $\zeta/l_d = 13.7$ % at $\sigma_{\text{sat}} = 263$ MPa; and at $T = 973$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.15/\text{mm}$ at $\sigma_{\text{cr}} = 188$ MPa to $\varphi = 7.1/\text{mm}$ at $\sigma_{\text{sat}} = 263$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 57.2$ % at $\sigma_{\text{cr}} = 188$ MPa to $\zeta/l_d = 34.5$ % at $\sigma_{\text{sat}} = 263$ MPa.

At $T = 1073$ K, the matrix multi-cracking density increases from $\varphi = 0.35/\text{mm}$ at $\sigma_{\text{cr}} = 169$ MPa to $\varphi = 9.4/\text{mm}$ at $\sigma_{\text{sat}} = 236$ MPa; at $T = 1073$ K and $t = 1$ h, the matrix multi-cracking density increases from $\varphi = 0.2/\text{mm}$ at $\sigma_{\text{cr}} = 169$ MPa to $\varphi = 7.7/\text{mm}$ at $\sigma_{\text{sat}} = 236$ MPa, and the

interface oxidation ratio decreases from $\zeta/l_d = 65.7$ % at $\sigma_{\text{cr}} = 169$ MPa to $\zeta/l_d = 33.2$ % at $\sigma_{\text{sat}} = 236$ MPa; and at $T = 1073$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.11/\text{mm}$ at $\sigma_{\text{cr}} = 169$ MPa to $\varphi = 5.2/\text{mm}$ at $\sigma_{\text{sat}} = 236$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 1$ at $\sigma_{\text{cr}} = 169$ MPa to $\zeta/l_d = 68.1$ % at $\sigma_{\text{sat}} = 236$ MPa.

The mini SiC/SiC composite

Zhang et al. [30] investigated the damage evolution of the matrix multi-cracking in the mini-SiC/SiC composite. At room temperature, the matrix multi-cracking evolution starts from the applied stress of $\sigma_{\text{cr}} = 135$ MPa and approaches saturation at $\sigma_{\text{sat}} = 250$ MPa; the matrix multi-cracking density increases from $\varphi = 0.4/\text{mm}$ to $\varphi = 2.4/\text{mm}$.

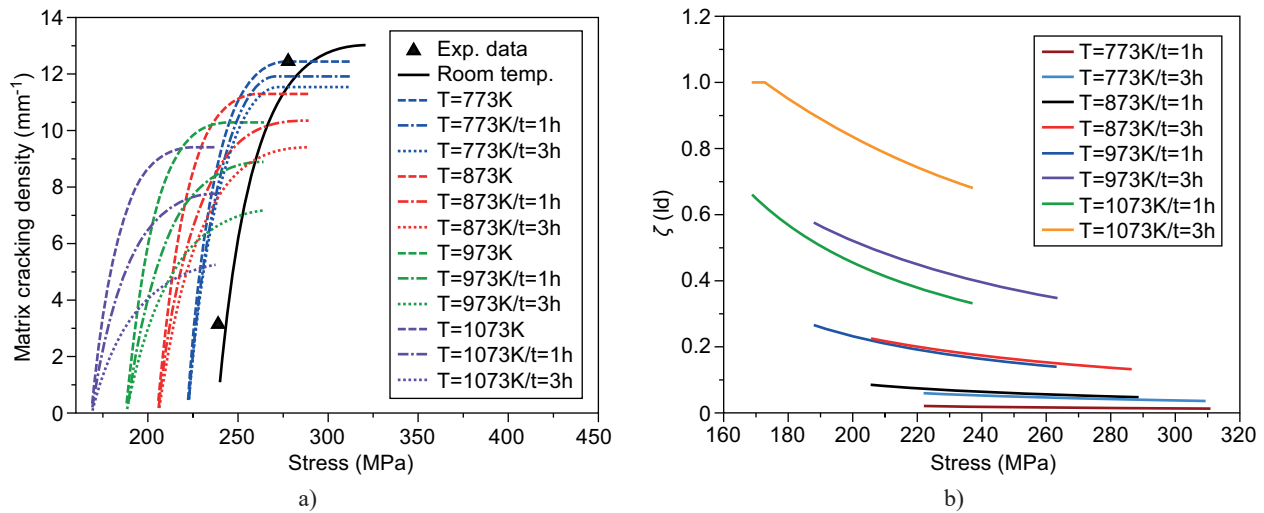


Figure 8. The experimental and theoretical matrix cracking density versus the applied stress curves for the different oxidation temperature and time (a); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time of the unidirectional SiC/SiC composite (b).

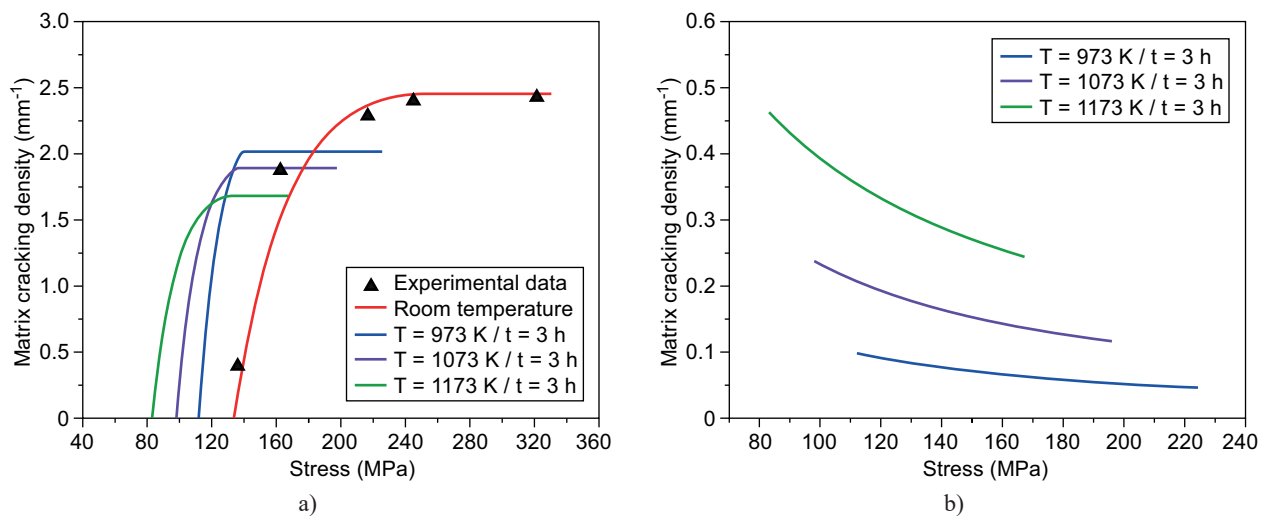


Figure 9. The experimental and theoretical matrix cracking density versus the applied stress curves for the different oxidation temperature and time (a); the interface oxidation ratio versus the applied stress curves for the different oxidation temperature and time of the mini SiC/SiC composite (b).

At $T = 973$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.06/\text{mm}$ at $\sigma_{\text{cr}} = 112$ MPa to $\varphi = 2/\text{mm}$ at $\sigma_{\text{sat}} = 140$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 9.8\%$ to $\zeta/l_d = 4.6\%$.

At $T = 1073$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.04/\text{mm}$ at $\sigma_{\text{cr}} = 98.4$ MPa to $\varphi = 1.9/\text{mm}$ at $\sigma_{\text{sat}} = 136$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 23.7\%$ to $\zeta/l_d = 11.6\%$.

At $T = 1173$ K and $t = 3$ h, the matrix multi-cracking density increases from $\varphi = 0.03/\text{mm}$ at $\sigma_{\text{cr}} = 83.4$ MPa to $\varphi = 1.7/\text{mm}$ at $\sigma_{\text{sat}} = 133$ MPa, and the interface oxidation ratio decreases from $\zeta/l_d = 46.2\%$ to $\zeta/l_d = 24.5\%$.

CONCLUSIONS

In this paper, the time-dependent matrix multi-cracking of SiC/SiC composite has been investigated considering the fibre/matrix interface oxidation. The effects of the fibre volume fraction, the fibre/matrix interface shear stress, the fibre/matrix interface frictional coefficient, the fibre/matrix interface de-bonded energy and the matrix fracture energy on the matrix multi-cracking density and the fibre/matrix interface oxidation ratio of the SiC/SiC composite have been discussed for the different temperatures and oxidation time. The experimental matrix multi-cracking density and the fibre/matrix interface oxidation ratio for the unidirectional and mini SiC/SiC composite at the different testing temperatures and oxidation time have been predicted. With an increasing temperature, the first matrix cracking stress of the SiC/SiC composite decreases due to the decreasing of the fibre/matrix interface shear stress in the de-bonded region.

With an increasing of oxidation time at an elevated temperature, the saturation matrix cracking density of the SiC/SiC composite decreases, due to the decreasing of the interface shear stress in the oxidation region.

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